

COMPUTATIONAL SEMANTICS: DAY 4

Johan Bos

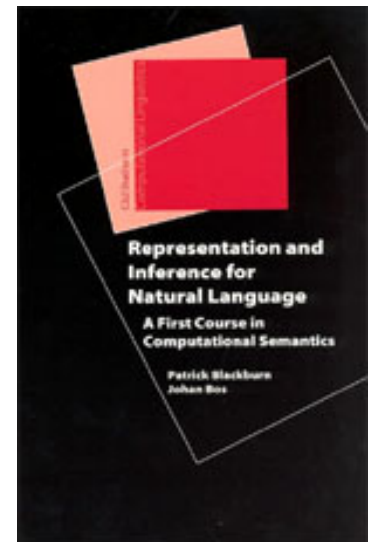
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Computational Semantics

- Day 1: Exploring Models
- Day 2: Meaning Representations
- Day 3: Computing Meanings with DCG
- **Day 4: Computing Meanings with CCG**
- Day 5: Drawing Inferences and Meaning Banking



Exercise 2 (homework)

- Look at the natural language statements associated with the images in GRIM
- Pick a frequently occurring verb that is not in the lexicon already
- Specify the lexical semantics of this verb in
 - a) no events (pre-Davidsonian)
 - b) Davidsonian
 - c) neo-Davidsonian
 - d) the spatial relations only

Questions after yesterday's lecture

- Some of the “white cats” were black... Why?
- Subsume lambdas from left to right?
E.g., what do you get after beta-converting

$\lambda x \lambda y \text{HEY}(y,x)@z$

YOU GET A
PARSER
FOR FREE
WITH
PROLOG!

NOT SURE IT IS
A PARSER I
WANT TO USE



Combinatory Categorical Grammar

- CCG is a lexicalised theory of grammar
 - Many different lexical categories
 - Few grammar rules (based on combinatory logic)
 - Covers complex cases of coordination and long-distance dependencies
- Not just theory, also used in practice
 - OpenCCG (Baldrige, White)
 - CCGbank (Hockenmaier)
 - C&C supertagger and parser (Clark, Curran)
 - Groningen Meaning Bank

Basic Categories

S	sentence
NP	noun phrase
N	noun
PP	prepositional phrase

Note: The category S comes with a feature to distinguish between various sentence mood and verb phrase forms.

Examples: S_{dcl} (declarative sentence)
 $S_{ng} \setminus NP$ (present participle)

Functor Categories

The direction of the slash determines where the argument appears:
forward slash (/): on its right; backward slash (\): on its left

NP/N	determiner
N/N	adjective
$S_{dcl} \backslash NP$	verb phrase (declarative mood)
$(S_{pt} \backslash NP) / NP$	transitive verb (present participle)
$(S_x \backslash NP) \backslash (S_x \backslash NP)$	adverb
$(N \backslash N) / NP$	preposition (modifying noun)

Example Lexicon

Word	Category
boy	: N
everything	: NP
the	: NP/N
eats	: $S_{dcl} \setminus NP$
eats	: $(S_{dcl} \setminus NP) / NP$
quickly	: $(S_X \setminus NP) \setminus (S_X \setminus NP)$

Application

Forward >

Backward <

Composition

(Generalised) Forward >**B**

(Generalised) Backward <**B**

Crossed Composition

(Generalised) Forward >**Bx**

(Generalised) Backward <**Bx**

Type Raising

Forward >**T**

Backward <**T**

Substitution

Forward >**S**

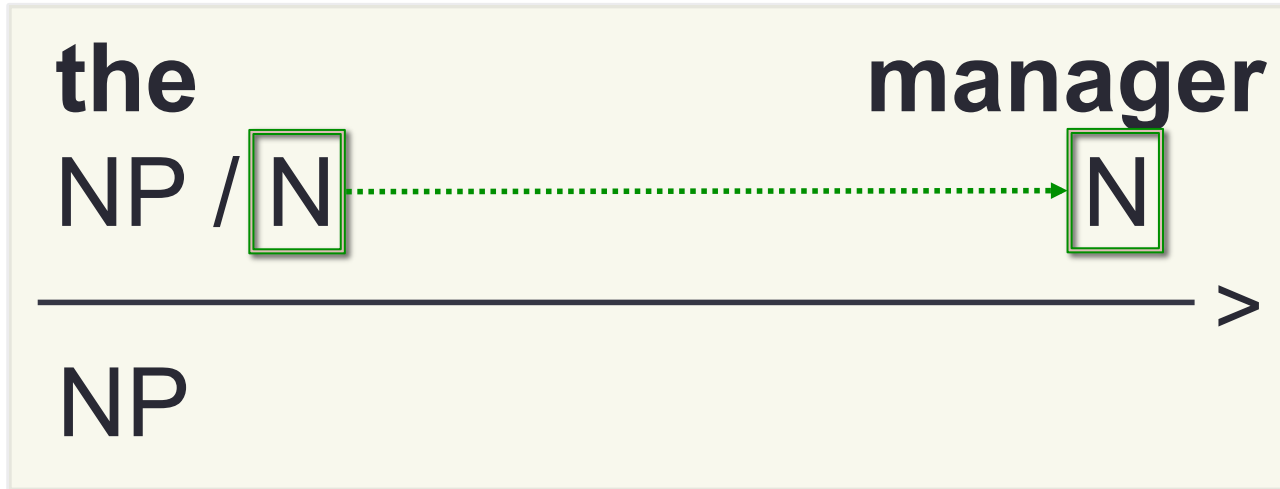
Backward <**S**

Crossed Substitution

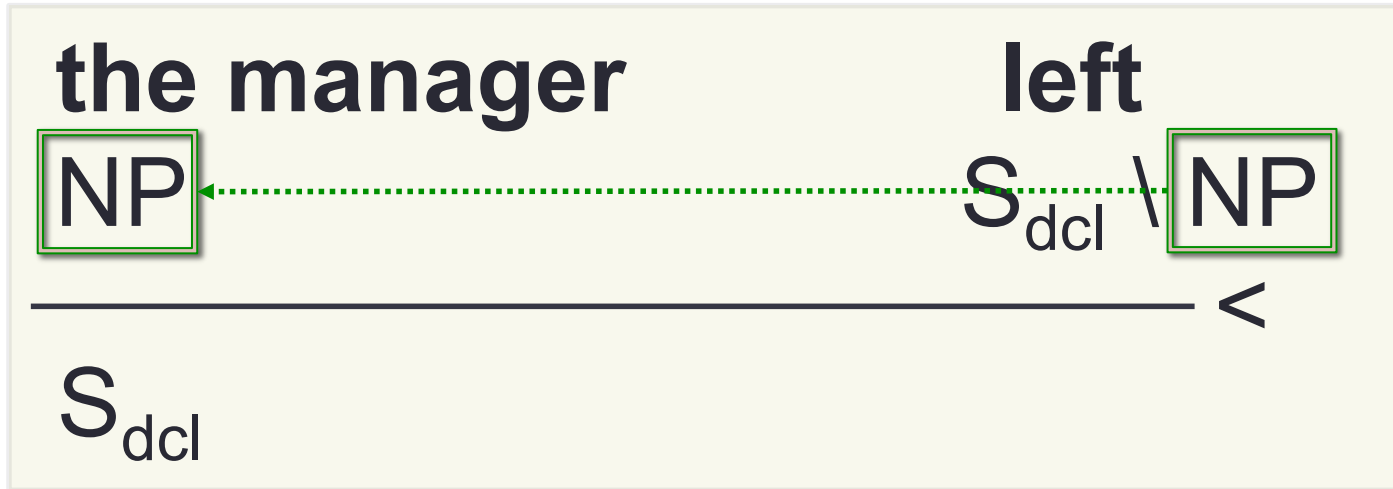
Forward >**Sx**

Backward <**Sx**

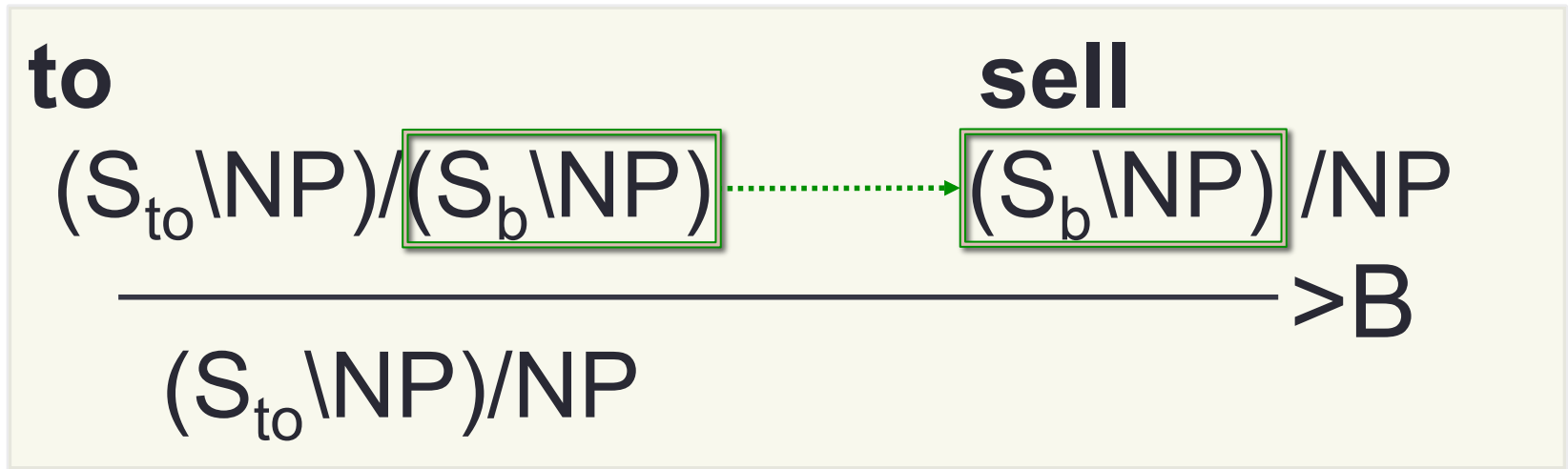
Combinatory Rules of CCG



Forward Application (>)



Backward Application ($<$)



Forward Composition (>B)

to

$(S_{to} \setminus NP) / (S_b \setminus NP)$

sell

$(S_b \setminus NP) / NP$

$(S_{to} \setminus NP) / NP$ $>B$

Forward Composition ($>B$)

...

John asked

curiously

$S_{dcl} \setminus S_{ynq}$

$S_{dcl} \setminus S_{dcl}$

$<B$

$S_{dcl} \setminus S_{ynq}$

Backward Composition ($<B$)

... **John asked**

$S_{dcl} \setminus S_{ynq}$

curiously

$S_{dcl} \setminus S_{dcl}$

<B

$S_{dcl} \setminus S_{ynq}$

Backward Composition (<B)

did

$(S_{dcl} \setminus NP) / (S_b \setminus NP)$

not

$(S_{dcl} \setminus NP) \setminus (S_{dcl} \setminus NP)$

$(S_{dcl} \setminus NP) / (S_b \setminus NP)$ <Bx

Backward Crossed Composition (<Bx)

did

$(S_{dcl} \setminus NP) / (S_b \setminus NP)$

not

$(S_{dcl} \setminus NP) \setminus (S_{dcl} \setminus NP)$

$\leq Bx$

$(S_{dcl} \setminus NP) / (S_b \setminus NP)$

Backward Crossed Composition ($\leq Bx$)

$$\frac{X/Y \quad Y}{X} >$$

$$\frac{Y \quad X \setminus Y}{X} <$$

$$\frac{X/Y \quad Y/Z}{X/Z} >B$$

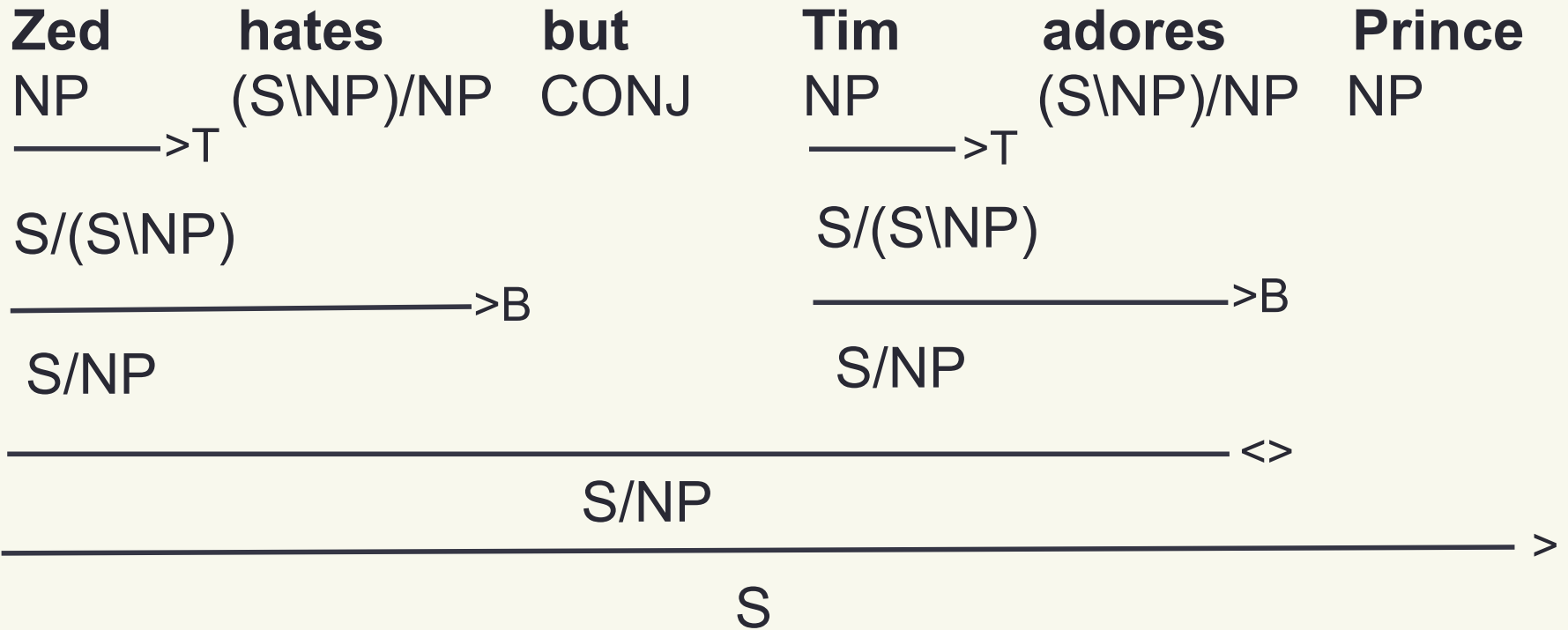
$$\frac{Y \setminus Z \quad X \setminus Y}{X \setminus Z} <B$$

$$\frac{X/Y \quad Y \setminus Z}{X \setminus Z} >Bx$$

$$\frac{Y/Z \quad X \setminus Y}{X/Z} <Bx$$

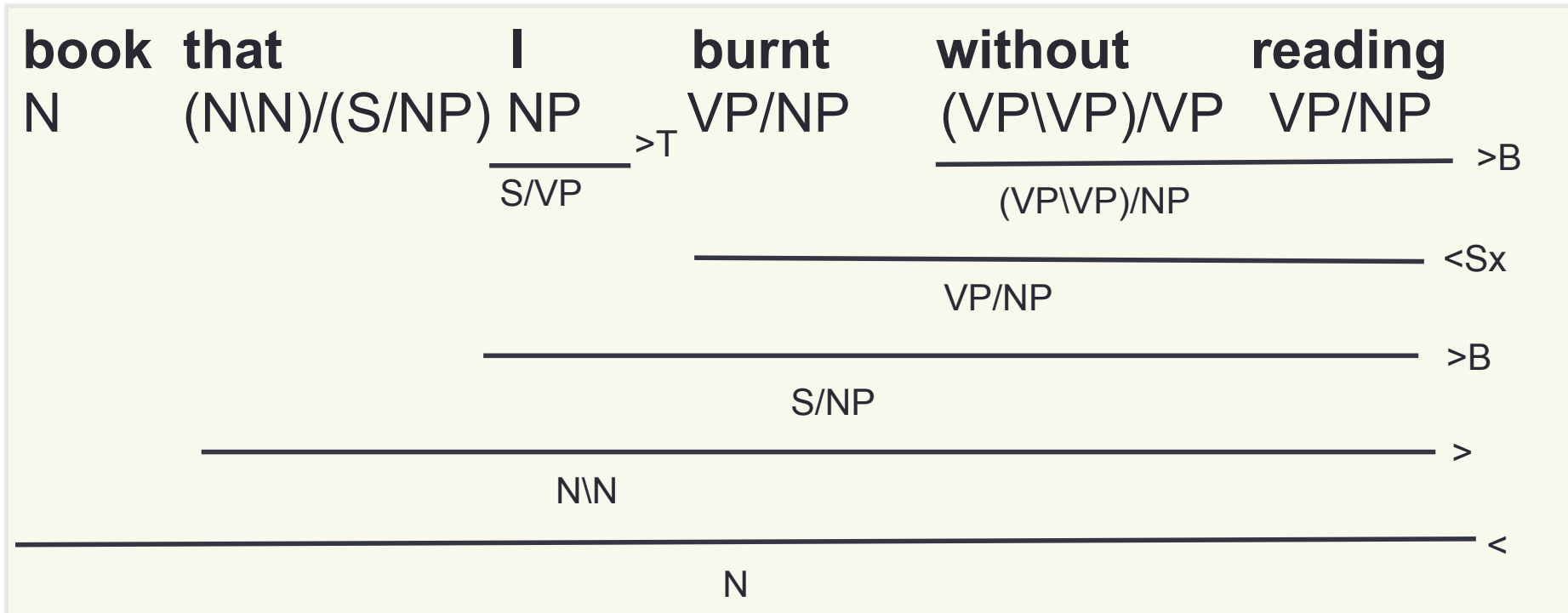


CCG rule schemata (1)



Type Raising (>T) and Coordination (<>)

Substitution (S), “parasitic gap”



Which paper did the professor read ... without understanding ... ?





$$\frac{X}{Y/(Y \setminus X)} >T$$

$$\frac{X}{X \setminus (Y/X)} <T$$

$$\frac{X \quad \text{CONJ} \quad X}{X} <>$$

$$\frac{(X/Y)/Z \quad Y/Z}{X/Z} >S$$

$$\frac{Y/Z \quad (X \setminus Y)/Z}{X/Z} <Sx$$



CCG rule schemata (2)



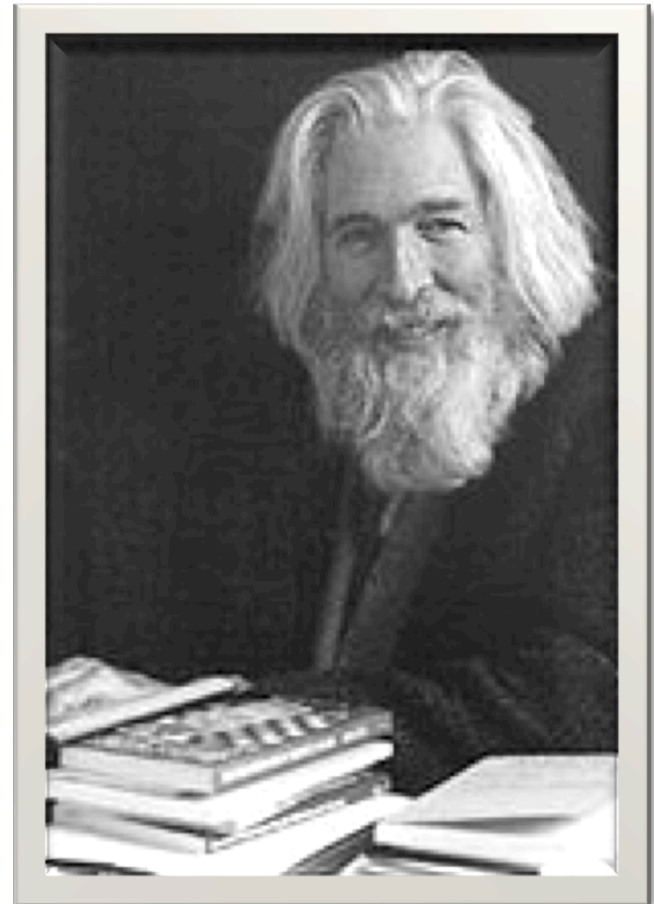
Bluebird



Starling



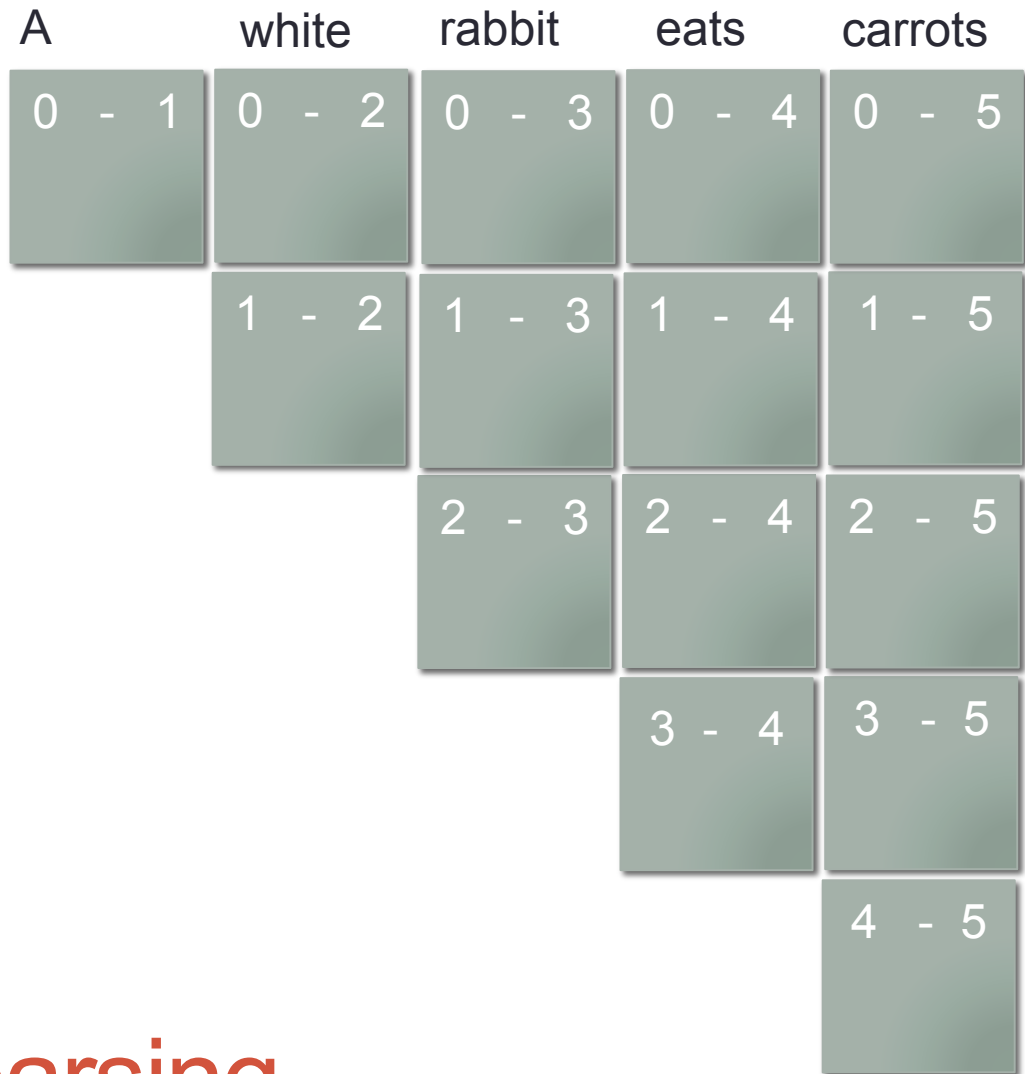
Thrush



Raymond Smullyan
to mock a mocking bird

CCG parsing

- top-down vs bottom-up
- CYK parsing
(John Cocke, Daniel Younger, Tadao Kasami)
- worst case running time: cubic on length of input string
(DCG are exponential)



CYK parsing

A	white	rabbit	eats	carrots
0 - 1	0 - 2	0 - 3	0 - 4	0 - 5
	1 - 2	1 - 3	1 - 4	1 - 5
		2 - 3	2 - 4	2 - 5
			3 - 4	3 - 5
				4 - 5



CYK parsing (S=1)

A	white	rabbit	eats	carrots
0 - 1 NP/N	0 - 2	0 - 3	0 - 4	0 - 5
	1 - 2 N/N	1 - 3	1 - 4	1 - 5
		2 - 3 N	2 - 4	2 - 5
			3 - 4 (SNP)/NP	3 - 5
				4 - 5 NP

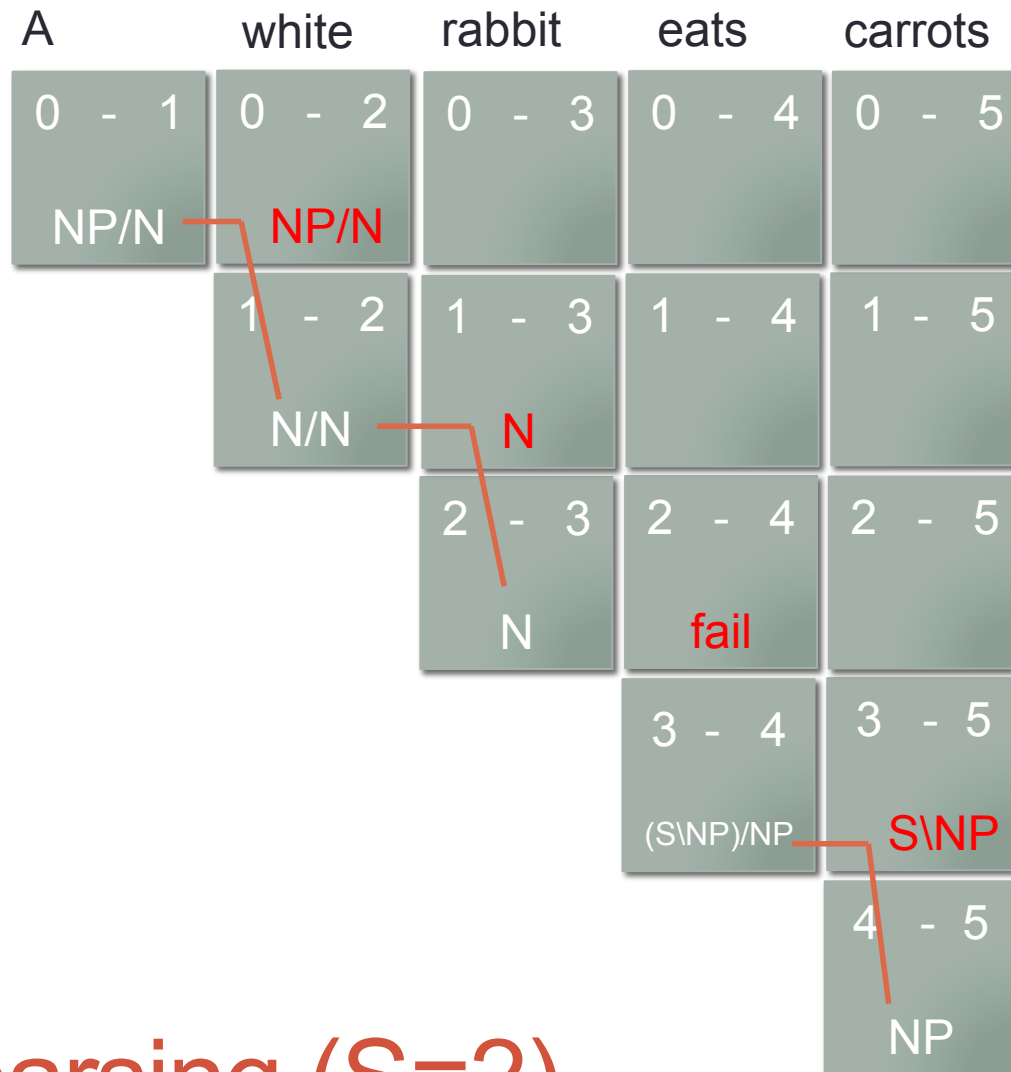


CYK parsing (S=1)

A	white	rabbit	eats	carrots
0 - 1 NP/N	0 - 2	0 - 3	0 - 4	0 - 5
	1 - 2 N/N	1 - 3	1 - 4	1 - 5
		2 - 3 N	2 - 4	2 - 5
			3 - 4 (SNP)/NP	3 - 5
				4 - 5 NP



CYK parsing (S=2)



CYK parsing (S=2)

A	white	rabbit	eats	carrots
0 - 1 NP/N	0 - 2 NP/N	0 - 3	0 - 4	0 - 5
	1 - 2 N/N	1 - 3 N	1 - 4	1 - 5
		2 - 3 N	2 - 4 fail	2 - 5
			3 - 4 (S\NP)/NP	3 - 5 S\NP
				4 - 5 NP



CYK parsing (S=3)

A	white	rabbit	eats	carrots
0 - 1 NP/N	0 - 2 NP/N	0 - 3 NP NP	0 - 4	0 - 5
	1 - 2 N/N	1 - 3 N	1 - 4 fail	1 - 5
		2 - 3 N	2 - 4 fail	2 - 5 fail
			3 - 4 (SNP)/NP	3 - 5 SNP
				4 - 5 NP



CYK parsing (S=3)

A	white	rabbit	eats	carrots
0 - 1 NP/N	0 - 2 NP/N	0 - 3 NP NP	0 - 4	0 - 5
	1 - 2 N/N	1 - 3 N	1 - 4 fail	1 - 5
		2 - 3 N	2 - 4 fail	2 - 5 fail
			3 - 4 (S\NP)/NP	3 - 5 S\NP
				4 - 5 NP



CYK parsing (S=4)



A	white	rabbit	eats	carrots
0 - 1 NP/N	0 - 2 NP/N	0 - 3 NP NP	0 - 4 fail	0 - 5
	1 - 2 N/N	1 - 3 N	1 - 4 fail	1 - 5 fail
		2 - 3 N	2 - 4 fail	2 - 5 fail
			3 - 4 (S\NP)/NP	3 - 5 S\NP
				4 - 5 NP

CYK parsing (S=4)

A	white	rabbit	eats	carrots
0 - 1 NP/N	0 - 2 NP/N	0 - 3 NP NP	0 - 4 fail	0 - 5
	1 - 2 N/N	1 - 3 N	1 - 4 fail	1 - 5 fail
		2 - 3 N	2 - 4 fail	2 - 5 fail
			3 - 4 (S\NP)/NP	3 - 5 S\NP
				4 - 5 NP



CYK parsing (S=5)

A	white	rabbit	eats	carrots
0 - 1 NP/N	0 - 2 NP/N	0 - 3 NP NP	0 - 4 fail	0 - 5 S
	1 - 2 N/N	1 - 3 N	1 - 4 fail	1 - 5 fail
		2 - 3 N	2 - 4 fail	2 - 5 fail
			3 - 4 (S\NP)/NP	3 - 5 S\NP
				4 - 5 NP



CYK parsing (S=5)

Provide CCG analyses

TRUE DESCRIPTIONS

- A white rabbit is eating a carrot.
- A rabbit with a carrot.
- A rabbit is nibbling on a carrot.
- A rabbit holding a carrot in its mouth.
- A carrot is being eaten by a rabbit.

FALSE DESCRIPTIONS

- A rabbit without a carrot.
- A brown rabbit is eating an orange carrot.
- Two rabbits are sharing a carrot.
- A carrot is holding a white rabbit.
- A rabbit with orange flowers.



Category	Partial DRS	Example
N	$\lambda x \text{ DOG}(x)$	<i>dog</i>
NP/N	$\lambda p \lambda q \exists x [(p@x) \& (q@x)]$	<i>a</i>
S\NP	$\lambda p (p@ \lambda y \text{ BARK}(y))$	<i>barked</i>

CCG: lexical semantics



Application ($>$ and $<$)

$$\frac{X/Y: \varphi \qquad Y: \psi}{X: (\varphi @ \psi)} \triangleright$$

$$\frac{Y: \psi \qquad X \setminus Y: \varphi}{X: (\varphi @ \psi)} \triangleleft$$

Application (\triangleright and \triangleleft)



Composition ($>B$ and $<B$)

$$\begin{array}{c}
 X/Y: \varphi \qquad Y/Z: \psi \\
 \hline
 X/Z: \lambda x. (\varphi @ (\psi @ x)) \quad >B
 \end{array}$$

$$\begin{array}{c}
 Y\backslash Z: \psi \qquad X\backslash Y: \varphi \\
 \hline
 X\backslash Z: \lambda x. (\varphi @ (\psi @ x)) \quad <B
 \end{array}$$

Composition ($>B$ and $<B$)

NP/N: **a**

N: **dog**

S\NP: **barked**

----- >

NP: **a dog**

----- <

S: **a dog barked**

A simple CCG derivation

NP/N: **a**

$\lambda p \lambda q \exists x[(p@x)\&(q@x)]$

N: **dog**

$\lambda z \text{DOG}(z)$

S\NP: **barked**

----- >

NP: **a dog**

----- <

S: **a dog barked**

A simple CCG derivation

NP/N: **a**

$\lambda p \lambda q \exists x[(p@x)\&(q@x)]$

N: **dog**

$\lambda z \text{DOG}(z)$

S\NP: **barked**

----- >

NP: **a dog**

$\lambda p \lambda q \exists x[(p@x)\&(q@x)] @ \lambda z \text{DOG}(z)$

----- <

S: **a dog barked**

A simple CCG derivation

NP/N: **a**

$\lambda p \lambda q \exists x[(p@x)\&(q@x)]$

N: **dog**

$\lambda z \text{DOG}(z)$

S\NP: **barked**

----- >

NP: **a dog**

$\lambda q \exists x[(\lambda z \text{DOG}(z)@x)\&(q@x)]$

----- <

S: **a dog barked**

A simple CCG derivation

NP/N: **a**

$\lambda p \lambda q \exists x[(p@x)\&(q@x)]$

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N: **dog**

$\lambda z \text{DOG}(z)$

S\NP: **barked**

$\lambda y \text{BARK}(y)$

----- >

NP: **a dog**

$\lambda q \exists x[\text{DOG}(x) \& (q@x)]$

----- <

S: **a dog barked**

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S\NP: **barked**

$\lambda p(p@\lambda y \text{BARK}(y))$

----- >

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----- <

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$\lambda p(p@\lambda y \text{BARK}(y)) @ \lambda q \exists x[\text{DOG}(x)\&(q@x)]$

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$\lambda z \text{DOG}(z)$

S\NP: **barked**

$\lambda p(p@ \lambda y \text{BARK}(y))$

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NP: **a dog**

$\lambda q \exists x[\text{DOG}(x) \& q@x]$

----- <

S: **a dog barked**

$(\lambda q \exists x[\text{DOG}(x) \& (q@x)]@ \lambda y \text{BARK}(y))$

A simple CCG derivation

NP/N: **a**

$\lambda p \lambda q \exists x[(p@x) \& (q@x)]$

N: **dog**

$\lambda z \text{DOG}(z)$

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$\lambda p(p@ \lambda y \text{BARK}(y))$

----- >

NP: **a dog**

$\lambda q \exists x[\text{DOG}(x) \& (q@x)]$

----- <

S: **a dog barked**

$\exists x[\text{DOG}(x) \& (\lambda y \text{BARK}(y)@x)]$

A simple CCG derivation

NP/N: **a**

$\lambda p \lambda q \exists x[(p@x) \& (q@x)]$

N: **dog**

$\lambda z \text{DOG}(z)$

S\NP: **barked**

$\lambda p(p@ \lambda y \text{BARK}(y))$

----- >

NP: **a dog**

$\lambda q \exists x[\text{DOG}(x) \& q@x]$

----- <

S: **a dog barked**

$\exists x[\text{DOG}(x) \& \text{BARK}(x)]$

A simple CCG derivation

Boxer demo

DirectPoll!

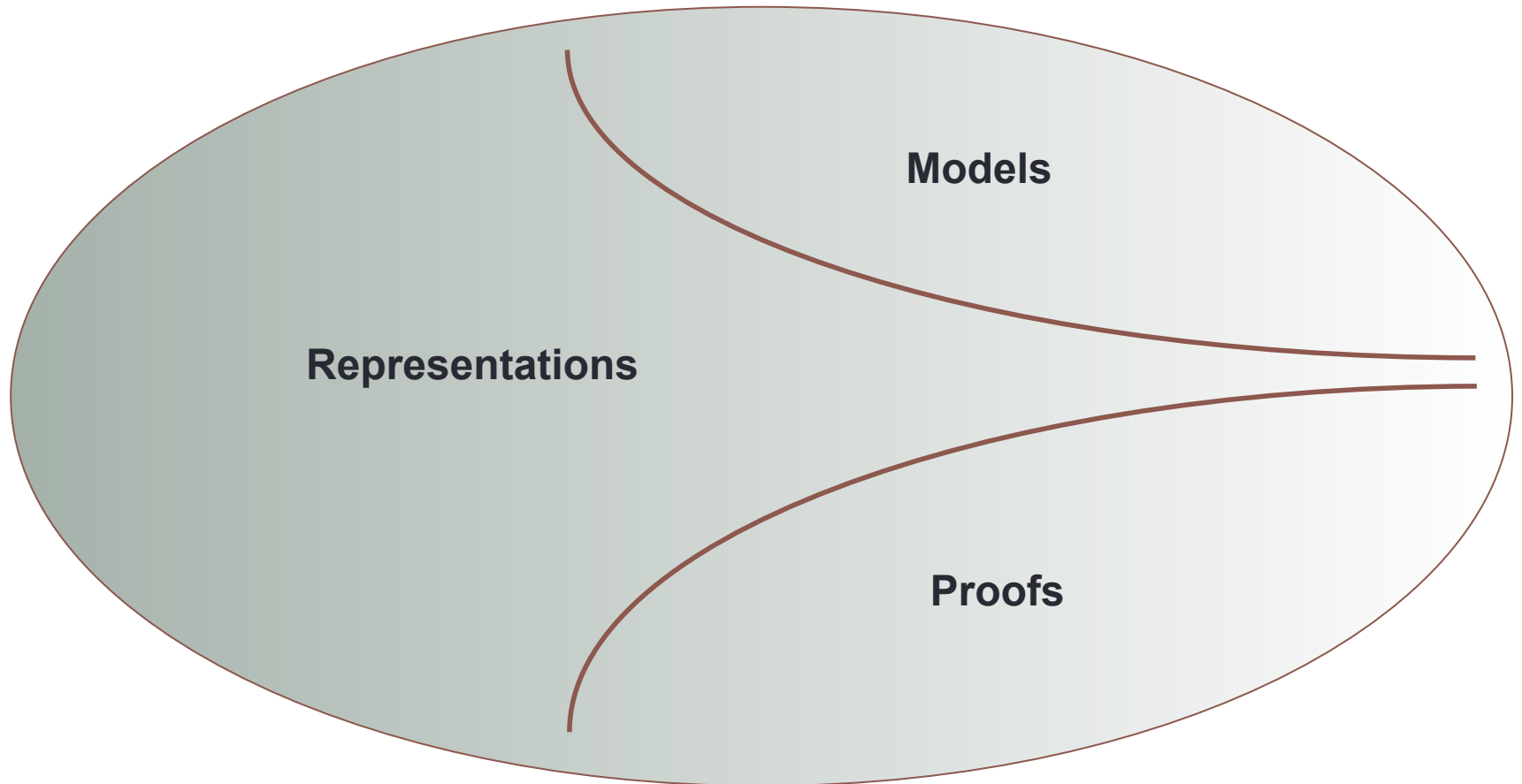
Computational Semantics Quiz

1. What event semantics representation does Boxer use?
 - a) Davidsonian
 - b) neo-Davidsonian
 - c) Hobbsian
2. $(\lambda x \text{WALK}(x)@vincent)$ is
 - a) a funny email address
 - b) a well-formed lambda-expression
 - c) a first-order formula
3. The expression $(\lambda x \text{LOVES}(x,x)@vincent)$
 - a) can be reduced to $\text{LOVES}(vincent,vincent)$
 - b) can be reduced to $\text{LOVES}(vincent,x)$
 - c) cannot be reduced

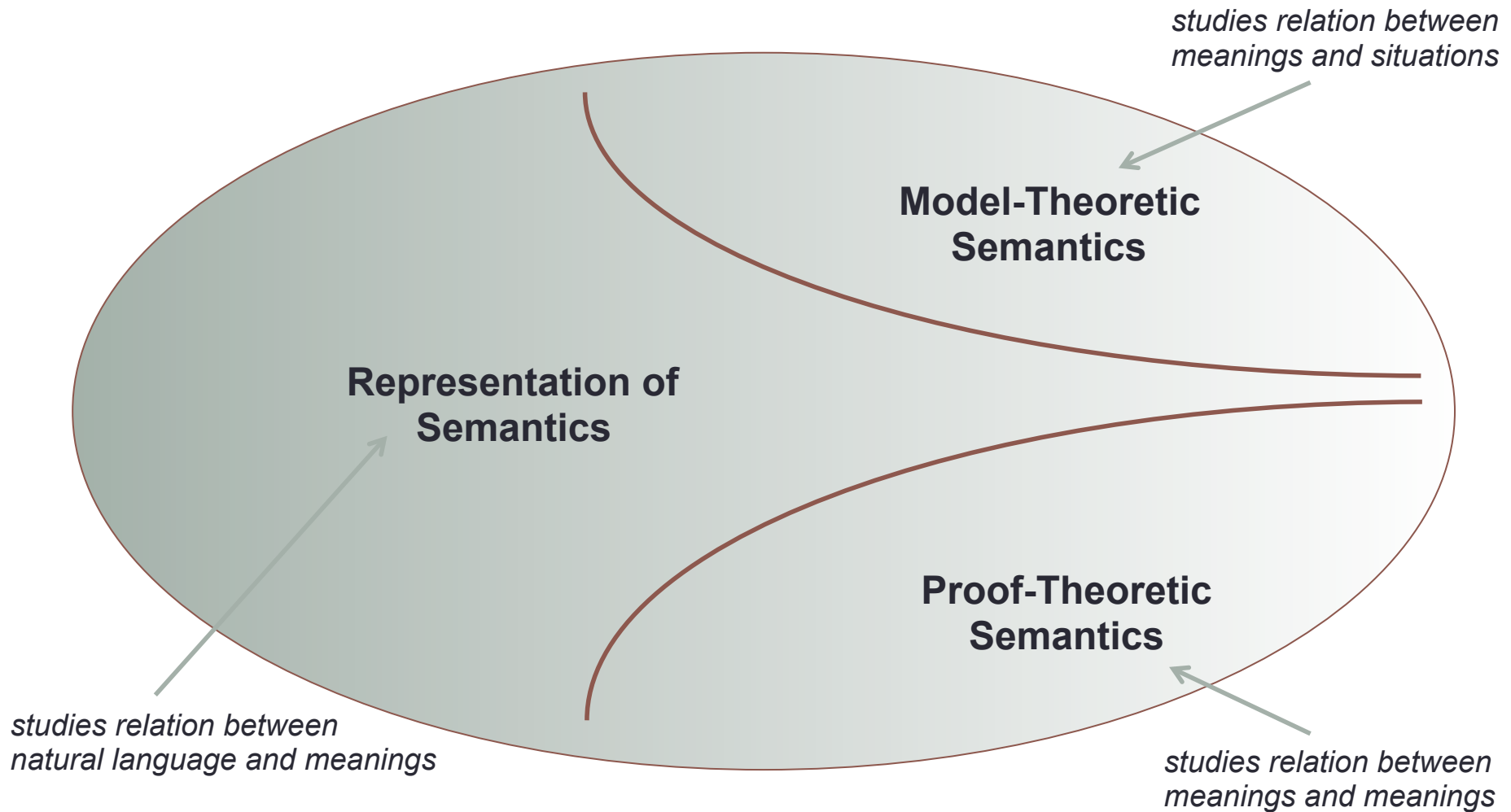
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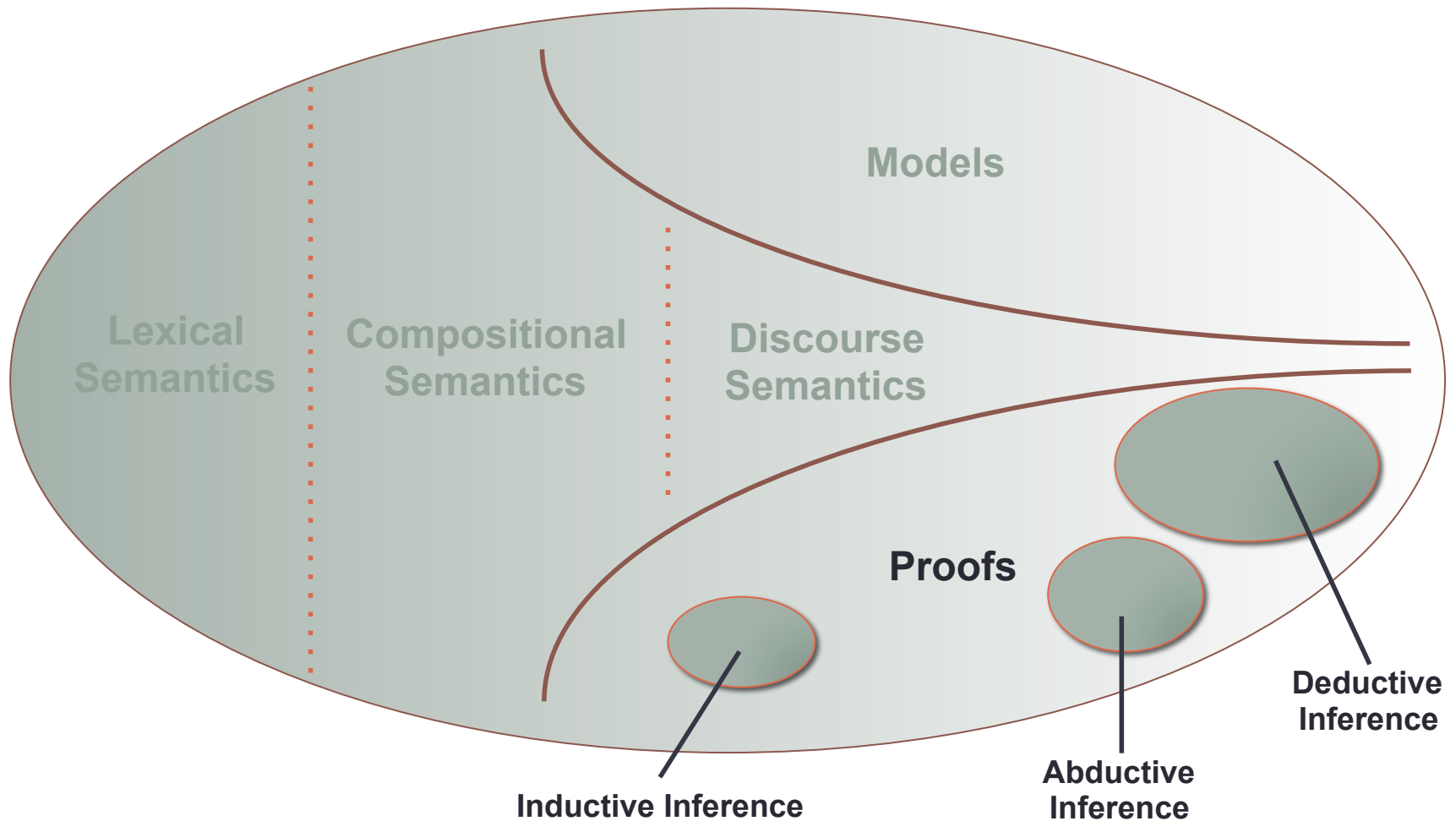
Planet Semantics



Planet Semantics



Proof-Theoretical Semantics



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