

Sequence Alignment

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Sequence alignment: Motivation

Motivation

- suppose we have no information except word lists
- goals:
 - estimate distances between languages
 - estimate cognate classes
 - track individual sound changes

Example

| Meaning | Italian | English | cognate |
|---------------|-----------|---------|---------|
| <i>few</i> | 'poco | fju: | 1 |
| <i>rub</i> | fre'gare | rʌb | 0 |
| <i>dull</i> | ot'tuzo | dʌl | 0 |
| <i>hunt</i> | kat'tfare | hʌnt | 0 |
| <i>year</i> | 'anno | jɪə | 0 |
| <i>this</i> | 'kwesto | ðɪs | 0 |
| <i>fish</i> | 'peʃʃe | fɪʃ | 1 |
| <i>rotten</i> | 'martʃo | 'rɒtən | 0 |
| <i>right</i> | 'dʒusto | raɪt | 0 |
| <i>when</i> | 'kwando | wen | 1 |
| <i>drink</i> | 'bere | drɪŋk | 0 |
| <i>heavy</i> | pe'sante | 'hevi | 0 |
| <i>heavy</i> | 'greve | 'hevi | 0 |
| <i>egg</i> | 'wɔvo | eg | 1 |
| <i>earth</i> | 'terra | ɜ:θ | 0 |
| <i>dust</i> | 'polvere | dʌst | 0 |
| <i>laugh</i> | 'ridere | la:f | 0 |
| <i>grass</i> | 'erba | gra:s | 0 |
| <i>sharp</i> | taλ'ʌnte | ʃa:p | 0 |
| <i>wash</i> | la'vere | wɒʃ | 0 |

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| <i>when</i> | 'kwando | wen | |
| <i>drink</i> | 'bere | drɪŋk | |
| <i>heavy</i> | pe'sante | 'hevi | |
| <i>heavy</i> | 'grɛve | 'hevi | |
| <i>egg</i> | 'wɔvo | eg | |
| <i>earth</i> | 'terra | ɜ:θ | |
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Preprocessing

- IPA is open-ended — 107 letters, 52 diacritics, 4 prosodic marks → 200,000 combinations
- good practice: map IPA strings to a uniform representation with fewer symbols
- common choices:
 - 10 Dolgopolsky sound classes (Dolgopolsky 1986; used i.a. in List 2014)
 - 41 ASJP sound classes
- this course: ASJP

| No. | Class | Description | Example |
|-----|-------|--|-----------|
| 1 | P | labial obstruents | p,b,f |
| 2 | T | dental obstruents | d,t,θ,ð |
| 3 | S | sibilants | s,z,ʃ,ʒ |
| 4 | K | velar obstruents, dental and alveolar affricates | k,g,ts,ʃt |
| 5 | M | labial nasal | m |
| 6 | N | remaining nasals | n,ŋ,ɳ |
| 7 | R | liquids | r,l |
| 8 | W | voiced labial fricative and initial rounded vowels | v,u |
| 9 | J | palatal approximant | j |
| 10 | ∅ | laryngeals and initial velar nasal | h,ɦ,ɳ |

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|---------------|----------|---------|
| <i>few</i> | poko | fyu |
| <i>rub</i> | fregare | rob |
| <i>dull</i> | ottuzzo | dol |
| <i>hunt</i> | kattSare | hunt |
| <i>year</i> | anno | yi3 |
| <i>this</i> | kwesto | 8is |
| <i>fish</i> | peSSe | fis |
| <i>rotten</i> | martSo | rot3n |
| <i>right</i> | dZusto | rait |
| <i>when</i> | kwando | wEn |
| <i>drink</i> | bere | driNk |
| <i>heavy</i> | pesante | hEvi |
| <i>heavy</i> | grEve | hEvi |
| <i>egg</i> | wovo | Eg |
| <i>earth</i> | tErra | 38 |
| <i>dust</i> | polvere | dost |
| <i>laugh</i> | ridere | lof |
| <i>grass</i> | Erba | gros |
| <i>sharp</i> | tallEnte | Sop |
| <i>wash</i> | lavare | woS |

Pairwise alignment

Levenshtein alignment

- related to as *edit distance*
- defines the distance between two strings as the minimal number of *edit operations* to transform one string into the other
- edit operations:
 - deletion
 - insertion
 - replacement
- example: grm. mEnS vs. Cimbrian menEs
 - 1 mEnS → menS (replace)
 - 2 menS → menES (insert)
 - 3 menES → menEs (insert)
- $d_L(\text{mEnS}, \text{menEs}) = 3$

Levenshtein alignment

- alternative presentation: alignment

| | | | | |
|---|---|---|---|---|
| m | E | n | - | S |
| | | | | |
| m | e | n | E | s |

- distance for a particular alignment is the number of non-identities
- Levenshtein distance is the number of mismatches for the optimal alignment

Computing the Levenshtein Distance

- recursive definition:

$$① \quad d_L(\epsilon, \alpha) = d_L(\alpha, \epsilon) = l(\alpha)$$

②

$$d_L(\alpha x, \beta y) = \min \begin{cases} d_L(\alpha, \beta) + \delta(x, y) \\ d_L(\alpha x, \beta) + 1 \\ d_L(\alpha, \beta y) + 1 \end{cases}$$

- apparently requires exponentially growing number of comparisons \Rightarrow computationally not feasible
- but:
 - if $l(\alpha) = n$ and $l(\beta) = m$, there are $n + 1$ substrings of α and $m + 1$ substrings of β
 - hence there are only $(n + 1)(m + 1)$ many different comparisons to be performed
 - computational complexity is polynomial (quadratic in $l(\alpha) + l(\beta)$)

Computing the Levenshtein distance

- Dynamic Programming

| | - | m | E | n | S |
|---|---|---|---|---|---|
| - | 0 | 1 | 2 | 3 | 4 |
| m | 1 | | | | |
| e | | 2 | | | |
| n | | | 3 | | |
| E | | | | 4 | |
| s | | | | | 5 |

Computing the Levenshtein distance

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| | - | m | E | n | S |
|---|---|---|---|---|---|
| - | 0 | 1 | 2 | 3 | 4 |
| m | 1 | | | | |
| e | | 2 | | | |
| n | | | 3 | | |
| E | | | | 4 | |
| s | | | | | 5 |

Computing the Levenshtein distance

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| | - | m | E | n | S |
|---|---|---|---|---|---|
| - | 0 | 1 | 2 | 3 | 4 |
| m | 1 | 0 | | | |
| e | | 2 | | | |
| n | | | 3 | | |
| E | | | | 4 | |
| s | | | | | 5 |

Computing the Levenshtein distance

- Dynamic Programming

| | - | m | E | n | S |
|---|---|------|---|---|---|
| - | 0 | 1 | 2 | 3 | 4 |
| m | 1 | 0 ↗↗ | | | |
| e | 2 | | | | |
| n | 3 | | | | |
| E | 4 | | | | |
| s | 5 | | | | |

Computing the Levenshtein distance

- Dynamic Programming

| | - | m | E | n | S |
|---|---|---|-----|---|---|
| - | 0 | 1 | 2 | 3 | 4 |
| m | 1 | 0 | ↖ ↘ | | |
| e | 2 | | | | |
| n | 3 | | | | |
| E | 4 | | | | |
| s | 5 | | | | |

Computing the Levenshtein distance

- Dynamic Programming

| | - | m | E | n | S |
|---|---|---|---|---|---|
| - | 0 | 1 | 2 | 3 | 4 |
| m | 1 | 0 | 1 | | |
| e | 2 | | | | |
| n | 3 | | | | |
| E | 4 | | | | |
| s | 5 | | | | |

Computing the Levenshtein distance

- Dynamic Programming

| | - | m | E | n | S |
|---|---|---|---|---|---|
| - | 0 | 1 | 2 | 3 | 4 |
| m | 1 | 0 | 1 | 2 | |
| e | 2 | | | | |
| n | 3 | | | | |
| E | 4 | | | | |
| s | 5 | | | | |

Computing the Levenshtein distance

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| | - | m | E | n | S |
|---|---|---|---|---|---|
| - | 0 | 1 | 2 | 3 | 4 |
| m | 1 | 0 | 1 | 2 | 3 |
| e | 2 | | | | |
| n | 3 | | | | |
| E | 4 | | | | |
| s | 5 | | | | |

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- Dynamic Programming

| | - | m | E | n | S |
|---|---|---|---|---|---|
| - | 0 | 1 | 2 | 3 | 4 |
| m | 1 | 0 | 1 | 2 | 3 |
| e | 2 | 1 | | | |
| n | 3 | | | | |
| E | 4 | | | | |
| s | 5 | | | | |

Computing the Levenshtein distance

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| | - | m | E | n | S |
|---|---|---|---|---|---|
| - | 0 | 1 | 2 | 3 | 4 |
| m | 1 | 0 | 1 | 2 | 3 |
| e | 2 | 1 | 1 | | |
| n | 3 | | | | |
| E | 4 | | | | |
| s | 5 | | | | |

Computing the Levenshtein distance

- Dynamic Programming

| | - | m | E | n | S |
|---|---|---|---|---|---|
| - | 0 | 1 | 2 | 3 | 4 |
| m | 1 | 0 | 1 | 2 | 3 |
| e | 2 | 1 | 1 | 2 | |
| n | 3 | | | | |
| E | 4 | | | | |
| s | 5 | | | | |

Computing the Levenshtein distance

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| | - | m | E | n | S |
|---|---|---|---|---|---|
| - | 0 | 1 | 2 | 3 | 4 |
| m | 1 | 0 | 1 | 2 | 3 |
| e | 2 | 1 | 1 | 2 | 3 |
| n | 3 | | | | |
| E | 4 | | | | |
| s | 5 | | | | |

Computing the Levenshtein distance

- Dynamic Programming

| | - | m | E | n | S |
|---|---|---|---|---|---|
| - | 0 | 1 | 2 | 3 | 4 |
| m | 1 | 0 | 1 | 2 | 3 |
| e | 2 | 1 | 1 | 2 | 3 |
| n | 3 | 2 | | | |
| E | 4 | | | | |
| s | 5 | | | | |

Computing the Levenshtein distance

- Dynamic Programming

| | - | m | E | n | S |
|---|---|---|---|---|---|
| - | 0 | 1 | 2 | 3 | 4 |
| m | 1 | 0 | 1 | 2 | 3 |
| e | 2 | 1 | 1 | 2 | 3 |
| n | 3 | 2 | 2 | | |
| E | 4 | | | | |
| s | 5 | | | | |

Computing the Levenshtein distance

- Dynamic Programming

| | - | m | E | n | S |
|---|---|---|---|---|---|
| - | 0 | 1 | 2 | 3 | 4 |
| m | 1 | 0 | 1 | 2 | 3 |
| e | 2 | 1 | 1 | 2 | 3 |
| n | 3 | 2 | 2 | 1 | |
| E | 4 | | | | |
| s | 5 | | | | |

Computing the Levenshtein distance

- Dynamic Programming

| | - | m | E | n | S |
|---|---|---|---|---|---|
| - | 0 | 1 | 2 | 3 | 4 |
| m | 1 | 0 | 1 | 2 | 3 |
| e | 2 | 1 | 1 | 2 | 3 |
| n | 3 | 2 | 2 | 1 | 2 |
| E | 4 | | | | |
| s | 5 | | | | |

Computing the Levenshtein distance

- Dynamic Programming

| | – | m | E | n | S |
|---|---|---|---|---|---|
| – | 0 | 1 | 2 | 3 | 4 |
| m | 1 | 0 | 1 | 2 | 3 |
| e | 2 | 1 | 1 | 2 | 3 |
| n | 3 | 2 | 2 | 1 | 2 |
| E | 4 | 3 | | | |
| s | 5 | | | | |

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- Dynamic Programming

| | - | m | E | n | S |
|---|---|---|---|---|---|
| - | 0 | 1 | 2 | 3 | 4 |
| m | 1 | 0 | 1 | 2 | 3 |
| e | 2 | 1 | 1 | 2 | 3 |
| n | 3 | 2 | 2 | 1 | 2 |
| E | 4 | 3 | 2 | | |
| s | 5 | | | | |

Computing the Levenshtein distance

- Dynamic Programming

| | - | m | E | n | S |
|---|---|---|---|---|---|
| - | 0 | 1 | 2 | 3 | 4 |
| m | 1 | 0 | 1 | 2 | 3 |
| e | 2 | 1 | 1 | 2 | 3 |
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| | - | m | E | n | S |
|---|---|---|---|---|---|
| - | 0 | 1 | 2 | 3 | 4 |
| m | 1 | 0 | 1 | 2 | 3 |
| e | 2 | 1 | 1 | 2 | 3 |
| n | 3 | 2 | 2 | 1 | 2 |
| E | 4 | 3 | 2 | 2 | 2 |
| s | 5 | | | | |

Computing the Levenshtein distance

- Dynamic Programming

| | - | m | E | n | S |
|---|---|---|---|---|---|
| - | 0 | 1 | 2 | 3 | 4 |
| m | 1 | 0 | 1 | 2 | 3 |
| e | 2 | 1 | 1 | 2 | 3 |
| n | 3 | 2 | 2 | 1 | 2 |
| E | 4 | 3 | 2 | 2 | 2 |
| s | 5 | 4 | | | |

Computing the Levenshtein distance

- Dynamic Programming

| | - | m | E | n | S |
|---|---|---|---|---|---|
| - | 0 | 1 | 2 | 3 | 4 |
| m | 1 | 0 | 1 | 2 | 3 |
| e | 2 | 1 | 1 | 2 | 3 |
| n | 3 | 2 | 2 | 1 | 2 |
| E | 4 | 3 | 2 | 2 | 2 |
| s | 5 | 4 | 3 | | |

Computing the Levenshtein distance

- Dynamic Programming

| | - | m | E | n | S |
|---|---|---|---|---|---|
| - | 0 | 1 | 2 | 3 | 4 |
| m | 1 | 0 | 1 | 2 | 3 |
| e | 2 | 1 | 1 | 2 | 3 |
| n | 3 | 2 | 2 | 1 | 2 |
| E | 4 | 3 | 2 | 2 | 2 |
| s | 5 | 4 | 3 | 3 | |

Computing the Levenshtein distance

- Dynamic Programming

| | - | m | E | n | S |
|---|---|---|---|---|---|
| - | 0 | 1 | 2 | 3 | 4 |
| m | 1 | 0 | 1 | 2 | 3 |
| e | 2 | 1 | 1 | 2 | 3 |
| n | 3 | 2 | 2 | 1 | 2 |
| E | 4 | 3 | 2 | 2 | 2 |
| s | 5 | 4 | 3 | 3 | 3 |

Computing the Levenshtein distance

- Dynamic Programming

| | - | m | E | n | S |
|---|---|---|---|---|----------|
| - | 0 | 1 | 2 | 3 | 4 |
| m | 1 | 0 | 1 | 2 | 3 |
| e | 2 | 1 | 1 | 2 | 3 |
| n | 3 | 2 | 2 | 1 | 2 |
| E | 4 | 3 | 2 | 2 | 2 |
| s | 5 | 4 | 3 | 3 | 3 |

- memorizing in each step which of the three cells to the left and above gave rise to the current entry lets us recover the corresponding optimal alignment

Computing the Levenshtein distance

- Dynamic Programming

| | - | m | E | n | S |
|---|---|---|---|---|---|
| - | 0 | 1 | 2 | 3 | 4 |
| m | 1 | 0 | 1 | 2 | 3 |
| e | 2 | 1 | 1 | 2 | 3 |
| n | 3 | 2 | 2 | 1 | 2 |
| E | 4 | 3 | 2 | 2 | 2 |
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| | - | m | E | n | S |
|---|---|---|---|---|---|
| - | 0 | 1 | 2 | 3 | 4 |
| m | 1 | 0 | 1 | 2 | 3 |
| e | 2 | 1 | 1 | 2 | 3 |
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| - | 0 | 1 | 2 | 3 | 4 |
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| e | 2 | 1 | 1 | 2 | 3 |
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| | - | m | E | n | S |
|---|---|---|---|---|---|
| - | 0 | 1 | 2 | 3 | 4 |
| m | 1 | 0 | 1 | 2 | 3 |
| e | 2 | 1 | 1 | 2 | 3 |
| n | 3 | 2 | 2 | 1 | 2 |
| E | 4 | 3 | 2 | 2 | 2 |
| s | 5 | 4 | 3 | 3 | 3 |

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Computing the Levenshtein distance

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| | - | m | E | n | S |
|---|---|---|---|---|---|
| - | 0 | 1 | 2 | 3 | 4 |
| m | 1 | 0 | 1 | 2 | 3 |
| e | 2 | 1 | 1 | 2 | 3 |
| n | 3 | 2 | 2 | 1 | 2 |
| E | 4 | 3 | 2 | 2 | 2 |
| s | 5 | 4 | 3 | 3 | 3 |

m E n - S
m e n E s

Computing the Levenshtein distance

| | - | m | E | n | S |
|---|---|---|---|---|---|
| - | 0 | 1 | 2 | 3 | 4 |
| m | 1 | 0 | 1 | 2 | 3 |
| e | 2 | 1 | 1 | 2 | 3 |
| n | 3 | 2 | 2 | 1 | 2 |
| E | 4 | 3 | 2 | 2 | 2 |
| s | 5 | 4 | 3 | 3 | 3 |

m E n - S
 m e n E s

| | - | m | E | n | S |
|---|---|---|---|---|---|
| - | 0 | 1 | 2 | 3 | 4 |
| m | 1 | 0 | 1 | 2 | 3 |
| e | 2 | 1 | 1 | 2 | 3 |
| n | 3 | 2 | 2 | 1 | 2 |
| E | 4 | 3 | 2 | 2 | 2 |
| s | 5 | 4 | 3 | 3 | 3 |

m E n S -
 m e n E s

Normalization for length

- grm. `mEnS` (*Mensch*, 'person') and Hindi `manuSya` are (partially) cognate
- grm. `ze3n` (*sehen*, 'see') and Hindi `deg` are not cognate
- still

$$d_L(\text{mEnS}, \text{manuSya}) = 4$$

$$d_L(\text{ze3n}, \text{deg}) = 3$$

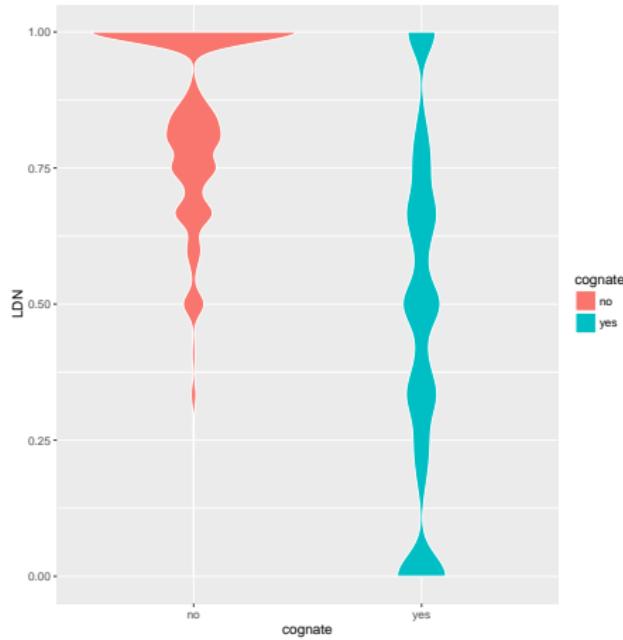
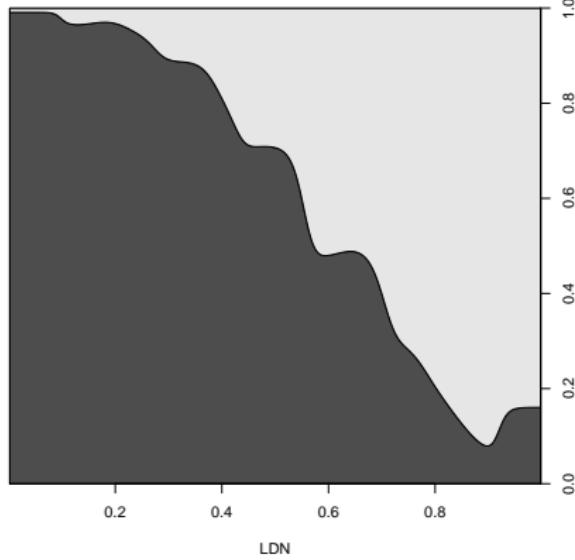
- normalization: dividing Levenshtein distance by length of longer string:

$$d_{LD}(\text{mEnS}, \text{manuSya}) = 4/7 \approx 0.57$$

$$d_{LD}(\text{ze3n}, \text{deg}) = 3/4 = 0.75$$

How well does normalized Levenshtein distance predict cognacy?

empirical probability of cognacy



Problems

- binary distinction: match vs. non-match
- frequently genuine sound correspondences in cognates are missed:

| | | | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| c | v | a | i | n | a | z | 3 | - | - | - | f | i | S |
| - | - | t | u | n | - | o | s | p | i | s | k | i | s |

- corresponding sounds count as mismatches even if they are aligned correctly

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| h | a | n | t | h | a | n | t |
| h | E | n | d | m | a | n | o |

- substantial amount of chance similarities

Background: probability theory

- Given two sequences: How likely is it that they are aligned?
- More general question: Given some data, and two competing hypotheses, how likely is it that the first hypothesis is correct?

Bayesian Inference!!!

- given:
 - data: d
 - hypotheses: h_1, h_0
 - model: $P(d|h_1), P(d|h_0)$
- wanted:

$$P(h_1|d) : P(h_0|d)$$

Bayesian inference

- Bayes Theorem:

$$P(h|d) = \frac{P(d|h)P(h)}{\sum_{h'} P(d|h')P(h')}$$

- ergo:

$$\begin{aligned} P(h_1|d) : P(h_0|d) &= P(d|h_1)P(h_1) : P(d|h_0)P(h_0) \\ P(h_1|d) : P(h_0|d) &= \frac{P(d|h_1)}{P(d|h_0)} \frac{P(h_1)}{P(h_0)} \\ \log(P(h_1|d) : P(h_0|d)) &= \log \frac{P(d|h_1)}{P(d|h_0)} + \log \frac{P(h_1)}{P(h_0)} \end{aligned}$$

Bayesian inference

- suppose we have many independent data: $\vec{d} = d_1, \dots, d_n$

$$P(\vec{d}|h) = \prod_{i=1}^n P(d_i|h)$$

$$\log P(\vec{d}|h) = \sum_{i=1}^n \log P(d_i|h)$$

$$\log \frac{P(\vec{d}|h_1)}{P(\vec{d}|h_0)} = \sum_{i=1}^n \log \frac{P(d_i|h_1)}{P(d_i|h_0)}$$

$$\log(P(h_1|\vec{d}) : P(h_0|\vec{d})) = \sum_{i=1}^n \log \frac{P(d_i|h_1)}{P(d_i|h_0)} + \log \frac{P(h_1)}{P(h_0)}$$

Bayesian inference

- mein argument against using Bayes' rule: the **prior probabilities** $P(h_1), P(h_0)$ are not known
- there are various heuristics, but no generally accepted way to obtain them
- if n is large though, $\log^{P(h_1)/P(h_0)}$ doesn't matter very much:¹

$$\log(P(h_1|\vec{d}) : P(h_0|\vec{d})) \approx \sum_{i=1}^n \log \frac{P(d_i|h_1)}{P(d_i|h_0)} = \log(P(\vec{d}|h_1) : P(\vec{d}|h_0))$$

- the quantity $\log(P(\vec{d}|h_1) : P(\vec{d}|h_0))$ is called **log-odds**

¹Also, if we choose an *uninformative prior* with $P(h_1) = P(h_0)$, we have $\log^{P(h_1)/P(h_0)} = 0$ anyway.

Log-odds

- log-odds can take any real value
- a positive value indicates evidence for h_1 and a negative value evidence for h_0
- the higher the absolute value, the stronger is the evidence

Weighted alignment

- suppose our data are two aligned sequences \vec{x}, \vec{y}
- for the time being, we assume there are no gaps in the alignment
 - h_1 : they developed from a common ancestor via substitutions
 - h_0 : they are unrelated
- additional assumptions (rough approximation in biology, pretty much off the mark in linguistics): substitutions in different positions occur independently

The null model

- if \vec{x} and \vec{y} are unrelated, their joint probability equals the product of their individual probabilities
- as a start (quite wrong both in biology and in linguistics): let us assume the strings have no “grammar”; each position is independent from all other positions
- then

$$P(\vec{x}, \vec{y}|h_0) = P(\vec{x}|h_0)P(\vec{y}|h_0)$$

$$= \prod_i P(x_i|h_0)P(y_i|h_0)$$

$$\log P(\vec{x}, \vec{y}|h_0) = \sum_i \log(P(x_i|h_0) + \log P(y_i|h_0))$$

The null model

- suppose \vec{x} and \vec{y} are generated by the same process (reasonable for DNA and protein comparison, false for cross-linguistic word comparison)
- then $P(x_i|h), P(y_i|h)$ are simply the probabilities of occurrence
- q_a : probability that symbol a occurs in a sequence

$$\log P(\vec{x}, \vec{y}|h_0) = \sum_i \log q_{x_i} + \sum_j \log q_{y_j}$$

- q can be estimated from relative frequencies

The alignment model

- suppose \vec{x} and \vec{y} evolved from a common ancestor via independent substitution mutations
- independence between positions:

$$P(\vec{x}, \vec{y}|h_1) = \prod_i P(x_i, y_i|h_2)$$

- $p_{a,b}$: probability that a position in the latest common ancestor of x and y evolved into an a in sequence \vec{x} and into a b in sequence \vec{y}

$$P(\vec{x}, \vec{y}|h_1) = \prod_i p_{x_i, y_i}$$

$$\log P(\vec{x}, \vec{y}|h_1) = \sum_i \log p_{x_i, y_i}$$

The log-odds score

- taking things together, we have

$$\log(P(\vec{x}, \vec{y}|h_1) : P(\vec{x}, \vec{y}|h_0)) = \sum_i \log \frac{p_{x_i, y_i}}{q_{x_i} q_{y_i}}$$

- $\log \frac{p_{ab}}{q_a q_b}$: **score** of the alignment of a with b
- also goes by the name of **Pointwise Mutual Information (PMI)**
- assembled in a **PMI substitution matrix**

Substitution matrices

- in bioinformatics, several commonly used substitution matrices for nucleotids and proteins
- based on explicit models of evolution and careful empirical testing
- for nucleotids:

| | <i>A</i> | <i>G</i> | <i>T</i> | <i>C</i> |
|----------|----------|----------|----------|----------|
| <i>A</i> | 2 | -5 | -7 | -7 |
| <i>G</i> | -5 | 2 | -7 | -7 |
| <i>T</i> | -7 | -7 | 2 | -5 |
| <i>C</i> | -7 | -7 | -5 | 2 |

Substitution matrices

- for proteins: different matrices for different evolutionary distances
- for instance: BLOSUM50

| | A | R | N | D | C | Q | E | G | H | I | L | K | M | F | P | S | T | W | Y | V |
|---|----------|----------|----------|----------|-----------|----------|----------|----------|-----------|----------|----------|----------|----------|----------|-----------|----------|-----------|----|----------|----------|
| A | 5 | -2 | -1 | -2 | -1 | -1 | -1 | 0 | -2 | -1 | -2 | -1 | -1 | -3 | -1 | 1 | 0 | -3 | -2 | 0 |
| R | -2 | 7 | -1 | -2 | -4 | 1 | 0 | -3 | 0 | -4 | -3 | 3 | -2 | -3 | -3 | -1 | -1 | -3 | -1 | -3 |
| N | -1 | -1 | 7 | 2 | -2 | 0 | 0 | 0 | 1 | -3 | -4 | 0 | -2 | -4 | -2 | 1 | 0 | -4 | -2 | -3 |
| D | -2 | -2 | 2 | 8 | -4 | 0 | 2 | -1 | -1 | -4 | -4 | -1 | -4 | -5 | -1 | 0 | -1 | -5 | -3 | -4 |
| C | -1 | -4 | -2 | -4 | 13 | -3 | -3 | -3 | -3 | -2 | -2 | -3 | -2 | -2 | -4 | -1 | -1 | -5 | -3 | -1 |
| Q | -1 | 1 | 0 | 0 | -3 | 7 | 2 | -2 | 1 | -3 | -2 | 2 | 0 | -4 | -1 | 0 | -1 | -1 | -1 | -3 |
| E | -1 | 0 | 0 | 2 | -3 | 2 | 6 | -3 | 0 | -4 | -3 | 1 | -2 | -3 | -1 | -1 | -1 | -3 | -2 | -3 |
| G | 0 | -3 | 0 | -1 | -3 | -2 | -3 | 8 | -2 | -4 | -4 | -2 | -3 | -4 | -2 | 0 | -2 | -3 | -3 | -4 |
| H | -2 | 0 | 1 | -1 | -3 | 1 | 0 | -2 | 10 | -4 | -3 | 0 | -1 | -1 | -2 | -1 | -2 | -3 | 2 | -4 |
| I | -1 | -4 | -3 | -4 | -2 | -3 | -4 | -4 | -4 | 5 | 2 | -3 | 2 | 0 | -3 | -3 | -1 | -3 | -1 | 4 |
| L | -2 | -3 | -4 | -4 | -2 | -2 | -3 | -4 | -3 | 2 | 5 | -3 | 3 | 1 | -4 | -3 | -1 | -2 | -1 | 1 |
| K | -1 | 3 | 0 | -1 | -3 | 2 | 1 | -2 | 0 | -3 | -3 | 6 | -2 | -4 | -1 | 0 | -1 | -3 | -2 | -3 |
| M | -1 | -2 | -2 | -4 | -2 | 0 | -2 | -3 | -1 | 2 | 3 | -2 | 7 | 0 | -3 | -2 | -1 | -1 | 0 | 1 |
| F | -3 | -3 | -4 | -5 | -2 | -4 | -3 | -4 | -1 | 0 | 1 | -4 | 0 | 8 | -4 | -3 | -2 | 1 | 4 | -1 |
| P | -1 | -3 | -2 | -1 | -4 | -1 | -1 | -2 | -2 | -3 | -4 | -1 | -3 | -4 | 10 | -1 | -1 | -4 | -3 | -3 |
| S | 1 | -1 | 1 | 0 | -1 | 0 | -1 | 0 | -1 | -3 | -3 | 0 | -2 | -3 | -1 | 5 | 2 | -4 | -2 | -2 |
| T | 0 | -1 | 0 | -1 | -1 | -1 | -2 | -2 | -1 | -1 | -1 | -1 | -2 | -1 | 2 | 5 | -3 | -2 | 0 | |
| W | -3 | -3 | -4 | -5 | -5 | -1 | -3 | -3 | -3 | -2 | -3 | -1 | 1 | -4 | -4 | -3 | 15 | 2 | -3 | |
| Y | -2 | -1 | -2 | -3 | -3 | -1 | -2 | -3 | 2 | -1 | -1 | -2 | 0 | 4 | -3 | -2 | -2 | 2 | 8 | -1 |
| V | 0 | -3 | -3 | -4 | -1 | -3 | -3 | -4 | -4 | 4 | 1 | -3 | 1 | -1 | -3 | -2 | 0 | -3 | -1 | 5 |

Substitution matrix for the ASJP data

1. identify large sample of pairs of closely related languages (using expert information or heuristics based on aggregated Levenshtein distance)

An.NORTHERN_PHILIPPINES.CENTRAL_BONTOC

An.MESO-PHILIPPINE.NORTHERN_SORSOGON

WF.WESTERN_FLY.IAMEGA

WF.WESTERN_FLY.GAMAEWE

Pan.PANOAN.KASHIBO_BAJO_AGUAYTIA

Pan.PANOAN.KASHIBO_SAN_ALEJANDRO

AA.EASTERN_CUSHITIC.KAMBAATA_2

AA.EASTERN_CUSHITIC.HADIYYA_2

ST.BAI.QILIQIAO_BAI_2

ST.BAI.YUNLONG_BAI

An.SULAWESI.MANDAR

An.OCEANIC.RAGA

An.SULAWESI.TANETE

An.SAMA-BAJAW.BOEPINANG_BAJAU

UA.AZTECAN.NAHUATL_HUEYAPAN_TETELA_DEL_VOLCAN

UA.AZTECAN.NAHUATL CUENTEPEC_TEMIXCO

An.SOUTHERN_PHILIPPINES.KAGAYANEN

An.NORTHERN_PHILIPPINES.LIMOS_KALINGA

An.MESO-PHILIPPINE.CANIPAAN_PALAWAN

An.NORTHWEST_MALAYO-POLYNESIAN.LAHANAN

NC.BANTOID.LIFONGA

NC.BANTOID.BOMBOMA_2

IE.INDIC.WAD_PAGGA

IE.INDIC.TALAGANG_HINDKO

NC.BANTOID.LINGALA

NC.BANTOID.LIFONGA

An.CENTRAL_MALAYO-POLYNESIAN.BALILEDO

An.CENTRAL_MALAYO-POLYNESIAN.PALUE

AuA.MUNDA.HO

AuA.MUNDA.KORKU

MGe.GE-KAINGANG.KAYAPO

MGe.GE-KAINGANG.APINAYE

Substitution matrix for the ASJP data

2. pick a concept and a pair of related languages at random
 - languages: Pen.MAIDUAN.MAIDU_KONKAU, Pen.MAIDUAN.NE_MAIIDU
 - concept: *one*
3. find corresponding words from the two languages:
 - nisam, niSem
4. do Levenshtein alignment

| | | | | |
|---|---|---|---|---|
| n | i | s | a | m |
| n | i | S | e | m |

5. for each sound pair, count number of correspondences
 - nn: 1; ii: 1; sS; 1; ae: 1; mm: 1

Substitution matrix for the ASJP data

- steps 2-5 are repeated 100,000 times

| | | | | | |
|------|-------|--------|-------|------------|-----|
| klem | S3--v | ligini | kulox | Naltir---i | ... |
| klom | S37on | ji---p | Gulox | Naltirtiri | ... |
| a | a | 56,047 | : | : | : |
| i | i | 33,955 | 4 | 8 | 2 |
| u | u | 23,731 | 4 | a | 2 |
| n | n | 21,363 | G | t | 2 |
| o | o | 19,619 | i | ! | 2 |
| m | m | 18,263 | G | y | 2 |
| t | t | 16,975 | d | ! | 2 |
| k | k | 16,773 | s | G | 2 |
| e | e | 12,745 | Z | 5 | 2 |
| r | r | 11,601 | G | s | 2 |
| l | l | 11,377 | X | z | 2 |
| b | b | 8,965 | ! | k | 2 |
| s | s | 8,245 | q | 8 | 2 |
| d | d | 6,829 | a | ! | 2 |
| p | p | 6,681 | a | ! | 2 |
| w | w | 6,613 | ! | y | 2 |
| N | N | 6,275 | ! | E | 2 |
| h | h | 5,331 | j | G | 2 |
| y | y | 5,321 | G | i | 2 |
| 3 | 3 | 5,255 | E | ! | 2 |

Substitution matrix for the ASJP data

6. determine relative frequency of occurrence of each sound within the entire database

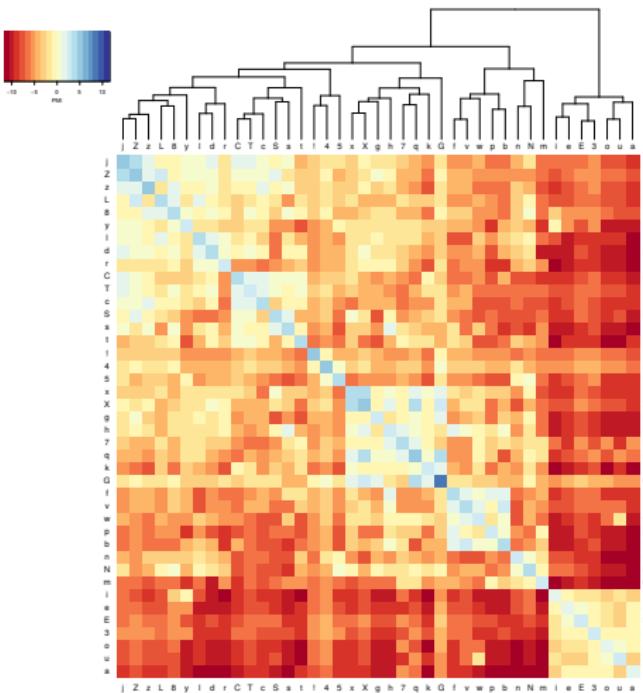
| | | | |
|---|--------|---|--------|
| a | 0.1479 | E | 0.0134 |
| i | 0.0969 | 7 | 0.0124 |
| u | 0.0696 | C | 0.0073 |
| o | 0.0626 | S | 0.0064 |
| n | 0.0614 | x | 0.0062 |
| e | 0.0478 | c | 0.0056 |
| k | 0.0478 | f | 0.0052 |
| m | 0.0465 | 5 | 0.0049 |
| t | 0.0449 | v | 0.0045 |
| r | 0.0346 | q | 0.0041 |
| l | 0.0331 | z | 0.0035 |
| b | 0.0248 | j | 0.0035 |
| s | 0.0243 | T | 0.0029 |
| w | 0.0232 | L | 0.0027 |
| 3 | 0.0228 | X | 0.0022 |
| y | 0.0222 | 8 | 0.0014 |
| d | 0.0214 | Z | 0.0011 |
| h | 0.0213 | ! | 0.0009 |
| p | 0.0202 | 4 | 0.0002 |
| N | 0.0201 | G | 0.0001 |
| g | 0.0178 | | |

Substitution matrix for the ASJP data

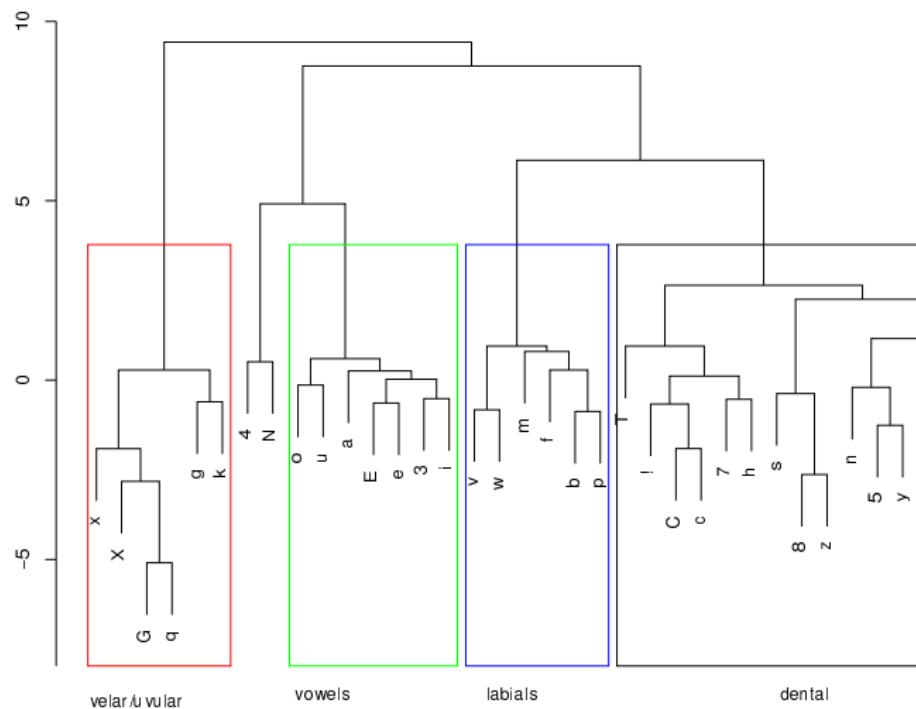
7. estimate p_{ab} as relative frequency of co-occurrence of a with b , q_a, q_b as individual relative frequencies, and determine PMI scores $\log_2 \frac{p_{ab}}{q_a q_b}$

| | | | | | | | | |
|----------|----------|---------------|----------|----------|---------------|-----|---|---------|
| G | G | 11.2348 | Z | j | 4.9386 | o | q | -3.2842 |
| ! | ! | 10.0202 | d | d | 4.9263 | C | a | -3.2893 |
| 4 | 4 | 9.1480 | g | g | 4.8958 | j | o | -3.2914 |
| 8 | 8 | 8.0650 | b | b | 4.8906 | a | m | -3.2915 |
| Z | Z | 7.9575 | s | s | 4.8277 | E | v | -3.3035 |
| X | X | 7.9375 | 4 | 5 | 4.7508 | ! | w | -3.3079 |
| L | L | 7.6276 | E | E | 4.7143 | ! | u | -3.3087 |
| z | z | 7.2624 | w | w | 4.6512 | 5 | q | -3.3116 |
| q | q | 7.2542 | h | h | 4.5819 | T | o | -3.3158 |
| f | f | 6.9117 | G | x | 4.5573 | ! | k | -3.3526 |
| v | v | 6.8418 | Z | z | 4.4943 | e | z | -3.3763 |
| 5 | 5 | 6.7731 | y | y | 4.4637 | ! | s | -3.3788 |
| j | j | 6.7587 | l | l | 4.4037 | ... | f | -3.3942 |
| T | T | 6.6580 | ! | G | 4.3760 | N | S | -3.3954 |
| S | S | 6.6054 | 3 | 3 | 4.3692 | ! | b | -3.4077 |
| c | c | 6.5989 | r | r | 4.3061 | L | b | -3.4558 |
| C | C | 6.2439 | X | q | 4.1200 | T | u | -3.4690 |
| 4 | G | 6.1943 | m | m | 4.1087 | 4 | i | -3.5529 |
| x | x | 6.1210 | t | t | 4.1021 | 5 | a | -3.8294 |
| G | X | 5.3342 | G | Z | 4.0429 | C | N | -3.8451 |
| G | q | 5.3017 | k | k | 3.9046 | ! | t | -4.2625 |
| 7 | 7 | 5.2111 | X | x | 3.8116 | ! | e | -4.3534 |
| p | p | 5.0693 | T | Z | 3.7380 | ! | i | -4.3712 |
| N | N | 4.9821 | 8 | G | 3.6993 | ! | a | -4.9817 |

Evaluation



Evaluation



Gap penalties

- gaps in an alignment correspond either to an insertion or a deletion
- simplified assumption: insertions and deletions are equally likely at all positions; symbols are inserted according to their general frequency of occurrence
- Suppose an item x_i is aligned to a gap. Let α be the probability that an insertion occurred since the latest common ancestor, and β the probability of a deletion

$$\begin{aligned} P(x_i, -|h_1) &= \alpha q_{x_i} + \beta q_{x_i} \\ P(x_i, -|h_0) &= q_{x_i} \\ \log(P(x_i, -|h_1) : P(x_i, -|h_0)) &= \log(\alpha + \beta) \\ &= -d \end{aligned}$$

- i.e., there is a constant term for each gap
- as $\alpha + \beta < 1$, this term is negative, i.e. there is a constant **penalty** for each gap

Affine gap penalties

- deletions/insertions frequently apply to entire blocks of symbols (both in biology and linguistics)
- probability of a gap of length n are higher than the product of probabilities of n individual gaps
- penalty e for **extending** a gap is lower than penalty d for **opening** a gap
- g : length of a gap

$$\gamma(g) = -d - (g - 1)e$$

- no principled way to derive the values of d and e ; have to be fixed via trial and error
- $d = 2.5$ and $e = 1.6$ work quite well for the ASJP data

Weighted alignment

- so far, we assumed that the alignment between \vec{x} and \vec{y} is known
- to assess strength of evidence for h_1 given \vec{x}, \vec{y} , we need to consider all alignments between \vec{x} and \vec{y}
- enumeration is infeasible, because the number of alignments between two sequences of length n is

$$\binom{2n}{n} = \frac{(2n)!}{(n!)^2} \approx \frac{2^{2n}}{\sqrt{\pi n}}$$

- computation is nonetheless possible using *Pair Hidden Markov Models*
- simpler task: find the most likely alignment and determine its log-odds!

The Needleman-Wunsch algorithm

- almost identical to Levenshtein algorithm, except:
 - matches/mismatches are counted not as 1 and 0, but as log-odds scores of the corresponding symbol pair
 - insertions/deletions are counted as gap penalties
 - by convention, the similarity rather than the distance is counted, i.e. we try to find the alignment that maximizes the score
- let \vec{x} have length n , \vec{y} length m , s_{ab} be the log-odds score of a and b , and d/e the gap penalties

The Needleman-Wunsch algorithm

$$F(0, 0) = 0$$

$$G(0, 0) = 0$$

$$\forall i : 0 < i \leq n$$

$$F(i, 0) = F(i - 1, 0) + G(i - 1, 0)e + (1 - G(i - 1, 0))d$$

$$G(i, 0) = 1$$

$$\forall j : 0 < j \leq m :$$

$$F(0, j) = F(0, j - 1) + G(0, j - 1)e + (1 - G(0, j - 1))d$$

$$G(0, j) = 1$$

$$\forall i, j : 0 < i \leq n, 0 < j \leq m$$

$$F(i, j) = \max \begin{cases} F(i - 1, j) + G(i - 1, j)e + (1 - G(i - 1, j))d \\ F(i, j - 1) + G(i, j - 1)e + (1 - G(i, j - 1))d \\ F(i - 1, j - 1) + s_{x_i y_j} \end{cases}$$

$$G(i, j) = 0 \text{ if } \arg \max \begin{cases} F(i - 1, j) + G(i - 1, j)e + (1 - G(i - 1, j))d \\ F(i, j - 1) + G(i, j - 1)e + (1 - G(i, j - 1))d \\ F(i - 1, j - 1) + s_{x_i y_j} \end{cases} = 3$$

1 else

Finding the best alignment

- Dynamic Programming

| | - | m | E | n | S |
|---|------|------|------|------|------|
| - | 0 | -2.5 | -4.1 | -5.7 | -7.3 |
| m | -2.5 | | | | |
| e | -4.1 | | | | |
| n | -5.7 | | | | |
| E | -7.3 | | | | |
| s | -8.9 | | | | |

Finding the best alignment

- Dynamic Programming

| | - | m | E | n | S |
|---|------|------|------|------|------|
| - | 0 | -2.5 | -4.1 | -5.7 | -7.3 |
| m | -2.5 | | | | |
| e | -4.1 | | | | |
| n | -5.7 | | | | |
| E | -7.3 | | | | |
| s | -8.9 | | | | |

Finding the best alignment

- Dynamic Programming

| | - | m | E | n | S |
|---|------|------|------|------|------|
| - | 0 | -2.5 | -4.1 | -5.7 | -7.3 |
| m | -2.5 | | | | |
| e | -4.1 | | | | |
| n | -5.7 | | | | |
| E | -7.3 | | | | |
| s | -8.9 | | | | |

Finding the best alignment

- Dynamic Programming

| | - | m | E | n | S |
|---|------|------|------|------|------|
| - | 0 | -2.5 | -4.1 | -5.7 | -7.3 |
| m | -2.5 | 4.13 | | | |
| e | -4.1 | | | | |
| n | -5.7 | | | | |
| E | -7.3 | | | | |
| s | -8.9 | | | | |

Finding the best alignment

- Dynamic Programming

| | - | m | E | n | S |
|---|------|------|------|------|------|
| - | 0 | -2.5 | -4.1 | -5.7 | -7.3 |
| m | -2.5 | 4.13 | | | |
| e | | -4.1 | | | |
| n | | -5.7 | | | |
| E | | -7.3 | | | |
| s | | -8.9 | | | |

Finding the best alignment

- Dynamic Programming

| | - | m | E | n | S |
|---|------|------|------|------|------|
| - | 0 | -2.5 | -4.1 | -5.7 | -7.3 |
| m | -2.5 | 4.13 | | | |
| e | | -4.1 | | | |
| n | | -5.7 | | | |
| E | | -7.3 | | | |
| s | | -8.9 | | | |

Finding the best alignment

- Dynamic Programming

| | - | m | E | n | S |
|---|------|------|------|------|------|
| - | 0 | -2.5 | -4.1 | -5.7 | -7.3 |
| m | -2.5 | 4.13 | 1.53 | | |
| e | -4.1 | | | | |
| n | -5.7 | | | | |
| E | -7.3 | | | | |
| s | -8.9 | | | | |

Finding the best alignment

- Dynamic Programming

| | - | m | E | n | S |
|---|------|------|------|------|------|
| - | 0 | -2.5 | -4.1 | -5.7 | -7.3 |
| m | -2.5 | 4.13 | 1.53 | 0.03 | |
| e | -4.1 | | | | |
| n | -5.7 | | | | |
| E | -7.3 | | | | |
| s | -8.9 | | | | |

Finding the best alignment

- Dynamic Programming

| | – | m | E | n | S |
|---|------|------|------|------|-------|
| – | 0 | -2.5 | -4.1 | -5.7 | -7.3 |
| m | -2.5 | 4.13 | 1.53 | 0.03 | -1.47 |
| e | -4.1 | | | | |
| n | -5.7 | | | | |
| E | -7.3 | | | | |
| s | -8.9 | | | | |

Finding the best alignment

- Dynamic Programming

| | – | m | E | n | S |
|---|------|------|------|------|-------|
| – | 0 | -2.5 | -4.1 | -5.7 | -7.3 |
| m | -2.5 | 4.13 | 1.53 | 0.03 | -1.47 |
| e | -4.1 | 1.53 | | | |
| n | -5.7 | | | | |
| E | -7.3 | | | | |
| s | -8.9 | | | | |

Finding the best alignment

- Dynamic Programming

| | – | m | E | n | S |
|---|------|------|------|------|-------|
| – | 0 | -2.5 | -4.1 | -5.7 | -7.3 |
| m | -2.5 | 4.13 | 1.53 | 0.03 | -1.47 |
| e | -4.1 | 1.53 | 5.65 | | |
| n | -5.7 | | | | |
| E | -7.3 | | | | |
| s | -8.9 | | | | |

Finding the best alignment

- Dynamic Programming

| | – | m | E | n | S |
|---|------|------|------|------|-------|
| – | 0 | -2.5 | -4.1 | -5.7 | -7.3 |
| m | -2.5 | 4.13 | 1.53 | 0.03 | -1.47 |
| e | -4.1 | 1.53 | 5.65 | 3.05 | |
| n | -5.7 | | | | |
| E | -7.3 | | | | |
| s | -8.9 | | | | |

Finding the best alignment

- Dynamic Programming

| | – | m | E | n | S |
|---|------|------|------|------|-------|
| – | 0 | -2.5 | -4.1 | -5.7 | -7.3 |
| m | -2.5 | 4.13 | 1.53 | 0.03 | -1.47 |
| e | -4.1 | 1.53 | 5.65 | 3.05 | 1.55 |
| n | -5.7 | | | | |
| E | -7.3 | | | | |
| s | -8.9 | | | | |

Finding the best alignment

- Dynamic Programming

| | – | m | E | n | S |
|---|------|------|------|------|-------|
| – | 0 | -2.5 | -4.1 | -5.7 | -7.3 |
| m | -2.5 | 4.13 | 1.53 | 0.03 | -1.47 |
| e | -4.1 | 1.53 | 5.65 | 3.05 | 1.55 |
| n | -5.7 | 0.03 | | | |
| E | -7.3 | | | | |
| s | -8.9 | | | | |

Finding the best alignment

- Dynamic Programming

| | – | m | E | n | S |
|---|------|------|------|------|-------|
| – | 0 | -2.5 | -4.1 | -5.7 | -7.3 |
| m | -2.5 | 4.13 | 1.53 | 0.03 | -1.47 |
| e | -4.1 | 1.53 | 5.65 | 3.05 | 1.55 |
| n | -5.7 | 0.03 | 3.05 | | |
| E | -7.3 | | | | |
| s | -8.9 | | | | |

Finding the best alignment

- Dynamic Programming

| | – | m | E | n | S |
|---|------|------|------|------|-------|
| – | 0 | -2.5 | -4.1 | -5.7 | -7.3 |
| m | -2.5 | 4.13 | 1.53 | 0.03 | -1.47 |
| e | -4.1 | 1.53 | 5.65 | 3.05 | 1.55 |
| n | -5.7 | 0.03 | 3.05 | 9.2 | |
| E | -7.3 | | | | |
| s | -8.9 | | | | |

Finding the best alignment

- Dynamic Programming

| | – | m | E | n | S |
|---|------|------|------|------|-------|
| – | 0 | -2.5 | -4.1 | -5.7 | -7.3 |
| m | -2.5 | 4.13 | 1.53 | 0.03 | -1.47 |
| e | -4.1 | 1.53 | 5.65 | 3.05 | 1.55 |
| n | -5.7 | 0.03 | 3.05 | 9.2 | 6.6 |
| E | -7.3 | | | | |
| s | -8.9 | | | | |

Finding the best alignment

- Dynamic Programming

| | - | m | E | n | S |
|---|------|-------|------|------|-------|
| - | 0 | -2.5 | -4.1 | -5.7 | -7.3 |
| m | -2.5 | 4.13 | 1.53 | 0.03 | -1.47 |
| e | -4.1 | 1.53 | 5.65 | 3.05 | 1.55 |
| n | -5.7 | 0.03 | 3.05 | 9.2 | 6.6 |
| E | -7.3 | -1.47 | | | |
| s | -8.9 | | | | |

Finding the best alignment

- Dynamic Programming

| | - | m | E | n | S |
|---|------|-------|------|------|-------|
| - | 0 | -2.5 | -4.1 | -5.7 | -7.3 |
| m | -2.5 | 4.13 | 1.53 | 0.03 | -1.47 |
| e | -4.1 | 1.53 | 5.65 | 3.05 | 1.55 |
| n | -5.7 | 0.03 | 3.05 | 9.2 | 6.6 |
| E | -7.3 | -1.47 | 4.75 | | |
| s | -8.9 | | | | |

Finding the best alignment

- Dynamic Programming

| | - | m | E | n | S |
|---|------|-------|------|------|-------|
| - | 0 | -2.5 | -4.1 | -5.7 | -7.3 |
| m | -2.5 | 4.13 | 1.53 | 0.03 | -1.47 |
| e | -4.1 | 1.53 | 5.65 | 3.05 | 1.55 |
| n | -5.7 | 0.03 | 3.05 | 9.2 | 6.6 |
| E | -7.3 | -1.47 | 4.75 | 6.6 | |
| s | -8.9 | | | | |

Finding the best alignment

- Dynamic Programming

| | - | m | E | n | S |
|---|------|-------|------|------|-------|
| - | 0 | -2.5 | -4.1 | -5.7 | -7.3 |
| m | -2.5 | 4.13 | 1.53 | 0.03 | -1.47 |
| e | -4.1 | 1.53 | 5.65 | 3.05 | 1.55 |
| n | -5.7 | 0.03 | 3.05 | 9.2 | 6.6 |
| E | -7.3 | -1.47 | 4.75 | 6.6 | 7.62 |
| s | -8.9 | | | | |

Finding the best alignment

- Dynamic Programming

| | - | m | E | n | S |
|---|------|-------|------|------|-------|
| - | 0 | -2.5 | -4.1 | -5.7 | -7.3 |
| m | -2.5 | 4.13 | 1.53 | 0.03 | -1.47 |
| e | -4.1 | 1.53 | 5.65 | 3.05 | 1.55 |
| n | -5.7 | 0.03 | 3.05 | 9.2 | 6.6 |
| E | -7.3 | -1.47 | 4.75 | 6.6 | 7.62 |
| s | -8.9 | -2.97 | | | |

Finding the best alignment

- Dynamic Programming

| | - | m | E | n | S |
|---|------|-------|------|------|-------|
| - | 0 | -2.5 | -4.1 | -5.7 | -7.3 |
| m | -2.5 | 4.13 | 1.53 | 0.03 | -1.47 |
| e | -4.1 | 1.53 | 5.65 | 3.05 | 1.55 |
| n | -5.7 | 0.03 | 3.05 | 9.2 | 6.6 |
| E | -7.3 | -1.47 | 4.75 | 6.6 | 7.62 |
| s | -8.9 | -2.97 | 2.15 | | |

Finding the best alignment

- Dynamic Programming

| | - | m | E | n | S |
|---|------|-------|------|------|-------|
| - | 0 | -2.5 | -4.1 | -5.7 | -7.3 |
| m | -2.5 | 4.13 | 1.53 | 0.03 | -1.47 |
| e | -4.1 | 1.53 | 5.65 | 3.05 | 1.55 |
| n | -5.7 | 0.03 | 3.05 | 9.2 | 6.6 |
| E | -7.3 | -1.47 | 4.75 | 6.6 | 7.62 |
| s | -8.9 | -2.97 | 2.15 | 5.1 | |

Finding the best alignment

- Dynamic Programming

| | - | m | E | n | S |
|---|------|-------|------|------|-------|
| - | 0 | -2.5 | -4.1 | -5.7 | -7.3 |
| m | -2.5 | 4.13 | 1.53 | 0.03 | -1.47 |
| e | -4.1 | 1.53 | 5.65 | 3.05 | 1.55 |
| n | -5.7 | 0.03 | 3.05 | 9.2 | 6.6 |
| E | -7.3 | -1.47 | 4.75 | 6.6 | 7.62 |
| s | -8.9 | -2.97 | 2.15 | 5.1 | 8.84 |

Finding the best alignment

- Dynamic Programming

| | - | m | E | n | S |
|---|------|-------|------|------|-------|
| - | 0 | -2.5 | -4.1 | -5.7 | -7.3 |
| m | -2.5 | 4.13 | 1.53 | 0.03 | -1.47 |
| e | -4.1 | 1.53 | 5.65 | 3.05 | 1.55 |
| n | -5.7 | 0.03 | 3.05 | 9.2 | 6.6 |
| E | -7.3 | -1.47 | 4.75 | 6.6 | 7.62 |
| s | -8.9 | -2.97 | 2.15 | 5.1 | 8.84 |

- memorizing in each step which of the three cells to the left and above gave rise to the current entry lets us recover the corresponding optimal alignment

Finding the best alignment

- Dynamic Programming

| | - | m | E | n | S |
|---|------|-------|------|------|-------|
| - | 0 | -2.5 | -4.1 | -5.7 | -7.3 |
| m | -2.5 | 4.13 | 1.53 | 0.03 | -1.47 |
| e | -4.1 | 1.53 | 5.65 | 3.05 | 1.55 |
| n | -5.7 | 0.03 | 3.05 | 9.2 | 6.6 |
| E | -7.3 | -1.47 | 4.75 | 6.6 | 7.62 |
| s | -8.9 | -2.97 | 2.15 | 5.1 | 8.84 |

- memorizing in each step which of the three cells to the left and above gave rise to the current entry lets us recover the corresponding optimal alignment

Finding the best alignment

- Dynamic Programming

| | - | m | E | n | S |
|---|------|-------|------|------|-------|
| - | 0 | -2.5 | -4.1 | -5.7 | -7.3 |
| m | -2.5 | 4.13 | 1.53 | 0.03 | -1.47 |
| e | -4.1 | 1.53 | 5.65 | 3.05 | 1.55 |
| n | -5.7 | 0.03 | 3.05 | 9.2 | 6.6 |
| E | -7.3 | -1.47 | 4.75 | 6.6 | 7.62 |
| s | -8.9 | -2.97 | 2.15 | 5.1 | 8.84 |

- memorizing in each step which of the three cells to the left and above gave rise to the current entry lets us recover the corresponding optimal alignment

Finding the best alignment

- Dynamic Programming

| | - | m | E | n | S |
|---|------|-------|------|------|-------|
| - | 0 | -2.5 | -4.1 | -5.7 | -7.3 |
| m | -2.5 | 4.13 | 1.53 | 0.03 | -1.47 |
| e | -4.1 | 1.53 | 5.65 | 3.05 | 1.55 |
| n | -5.7 | 0.03 | 3.05 | 9.2 | 6.6 |
| E | -7.3 | -1.47 | 4.75 | 6.6 | 7.62 |
| s | -8.9 | -2.97 | 2.15 | 5.1 | 8.84 |

- memorizing in each step which of the three cells to the left and above gave rise to the current entry lets us recover the corresponding optimal alignment

Finding the best alignment

- Dynamic Programming

| | - | m | E | n | S |
|---|------|-------|------|------|-------|
| - | 0 | -2.5 | -4.1 | -5.7 | -7.3 |
| m | -2.5 | 4.13 | 1.53 | 0.03 | -1.47 |
| e | -4.1 | 1.53 | 5.65 | 3.05 | 1.55 |
| n | -5.7 | 0.03 | 3.05 | 9.2 | 6.6 |
| E | -7.3 | -1.47 | 4.75 | 6.6 | 7.62 |
| s | -8.9 | -2.97 | 2.15 | 5.1 | 8.84 |

- memorizing in each step which of the three cells to the left and above gave rise to the current entry lets us recover the corresponding optimal alignment

Evaluation

left: Levenshtein alignment; right: Needleman-Wunsch alignment

| | | | | | | |
|-----------|------------|--|---------|---------|---------|-----------|
| -iX | iX- | | -blat | b-lat | han-t | han-t |
| ego | ego | | folyu | folyu | manus | manus |
| du | du | | haut-- | haut-- | --brust | b--rust |
| tu | tu | | -kutis | k-utis | pektus- | pektus- |
| vir | vir | | ---blut | ---blut | leb3r | leb3r |
| nos | nos | | saNgwis | saNgwis | yekur | yekur |
| ains | ain-s | | knoX3n | knoX3n | triNk3n | triNk3n- |
| unus | -unus | | --o--s | --os-- | -bibere | -bi-bere |
| cvai | cvai | | horn- | horn- | --ze3n | --ze3n |
| -duo | duo- | | kornu | kornu | widere | widere |
| ---mEnS | mEnS--- | | -au-g3 | a-ug3- | -her3n | --her3n |
| persona | persona | | okulus | okulus | audire | audire- |
| ---fiS | fiS--- | | na-z3 | naz3- | Sterb3n | Sterb3n |
| piskis | piskis | | nasus | nasus | -mor--i | -mor-i- |
| hun-t | hun-t | | chan | chan- | khom3n | khom3n--- |
| kanis | kanis | | dens | d-ens | wenire | w---enire |
| -----laus | -----laus | | -chuN3 | chuN--3 | zon3 | zon3 |
| pedikulus | pedikul-us | | liNgwE | -liNgwE | so-l | sol- |

Evaluation

vas3r --vas3r
-akwa akwa---

Stain Sta-in
lapis -lapis

-foia fo-ia
iNnis iNnis

pfat p-fat
viya viya-

bErk bErk
mons mons

n-at na-t
noks noks

---fol fol----
plenus p-lenus

no--i no-i-
nowus nowus

nam-3 nam3-
nomen nomen

German — Swabian

| | | | | | | | |
|-----------|-------|----------|-------|-----------|-------|----------|-------|
| 'I': | 0.3 | 'louse': | 15.01 | 'tongue': | 9.8 | 'die': | 10.16 |
| iX | | laus | | chuN3 | | Sterb3n | |
| i | | laus | | cuN | | StEab | |
| 'you': | 8.26 | 'tree': | 6.57 | 'knee': | 7.77 | 'come': | 11.84 |
| du | | baum | | kni | | khom3n | |
| du | | bom | | knui | | khom | |
| 'we': | -1.09 | 'leaf': | 11.92 | 'hand': | 8.6 | 'sun': | 8.79 |
| vir | | blat | | hant | | zon3 | |
| mia | | blad | | hEnd | | sonE | |
| 'one': | 4.63 | 'skin': | 14.42 | 'breast': | 14.81 | 'star': | 16.16 |
| ains | | haut | | brust | | StErn | |
| ois | | haut | | bXuSt | | StEan | |
| 'two': | 16.0 | 'blood': | 12.88 | 'liver': | 10.01 | 'water': | 7.8 |
| cvai | | blut | | leb3r | | vas3r | |
| cvoi | | blud | | leba | | vaza | |
| 'person': | 12.61 | 'bone': | 16.88 | 'drink': | 4.99 | 'stone': | 10.36 |
| mEnS | | knoX3n | | triNk3n | | Stain | |
| mEnZE | | knoXE | | dXiNg | | Stoi | |
| 'fish': | 16.35 | 'horn': | 8.75 | 'see': | 0.63 | 'fire': | 12.43 |
| fiS | | horn | | ze3n | | foia | |
| fiS | | hoan | | se | | fuiia | |

German — English

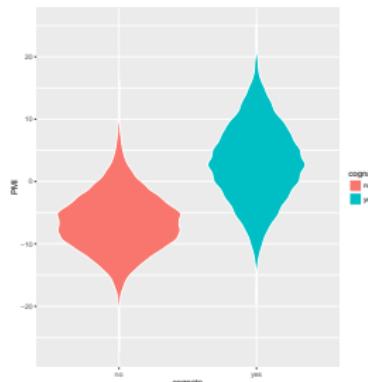
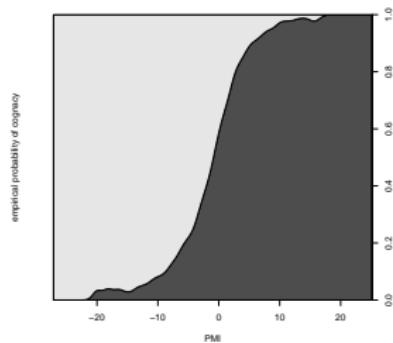
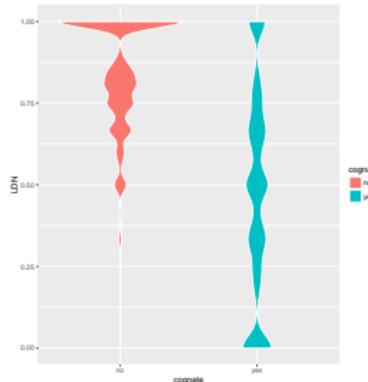
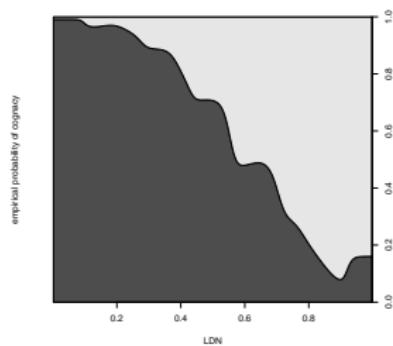
| | | | |
|-----------------------------|--------------------------------|-----------------------------------|----------------------------------|
| 'I': -2.3 iX Ei | 'tree': -7.83 baum tri | 'tongue': -0.63 chuN3 t3N | 'die': -7.7 Sterb3n dEi |
| 'you': 2.34 du yu | 'leaf': -0.47 blat lif | 'knee': 3.86 kni ni | 'come': 1.22 khom3n k3m |
| 'we': 2.21 vir wi | 'blood': 9.46 blut bl3d | 'hand': 8.6 hant hEnd | 'sun': 1.95 zon3 s3n |
| 'one': -2.3 ains w3n | 'bone': -1.36 knoX3n bon | 'breast': 16.93 brust brest | 'star': 8.2 StErn star |
| 'two': -5.25 cvai tu | 'horn': 15.73 horn horn | 'liver': 14.65 leb3r liv3r | 'water': 12.06 vas3r wat3r |
| 'fish': 16.35 fiS fiS | 'eye': -4.1 aug3 Ei | 'drink': 7.48 triNk3n drink | 'stone': 6.75 Stain ston |
| 'dog': -7.46 hunt dag | 'nose': 1.63 naz3 nos | 'see': -3.04 ze3n si | 'fire': 6.79 foia fEir |

German — Latin

| | | | |
|------------------------------------|-------------------------------------|-----------------------------------|-----------------------------------|
| 'I': -3.87 iX ego | 'louse': -0.08 laus pedikulus | 'nose': 4.49 naz3 nasus | 'see': -4.15 ze3n widere |
| 'you': 3.62 du tu | 'tree': -3.85 baum arbor | 'tooth': -2.78 chan dens | 'hear': -4.24 her3n audire |
| 'we': -5.06 vir nos | 'leaf': -3.57 blat folyu | 'tongue': -3.4 chuN3 liNgwE | 'die': -6.12 Sterb3n mori |
| 'one': 2.39 ains unus | 'skin': -0.25 haut kutis | 'knee': 0.8 kni genu | 'come': -9.25 khom3n wenire |
| 'two': -5.51 cvai duo | 'blood': -9.18 blut saNgwis | 'hand': 0.73 hant manus | 'sun': 0.97 zon3 sol |
| 'person': -4.66 mEnS persona | 'bone': -5.72 knoX3n os | 'breast': 1.39 brust pektus | 'star': 5.72 StErn stela |
| 'fish': 0.29 fiS piskis | 'horn': 7.55 horn kornu | 'liver': 5.37 leb3r yekur | 'water': -5.4 vas3r akwa |

How well does PMI similarity predict cognacy?

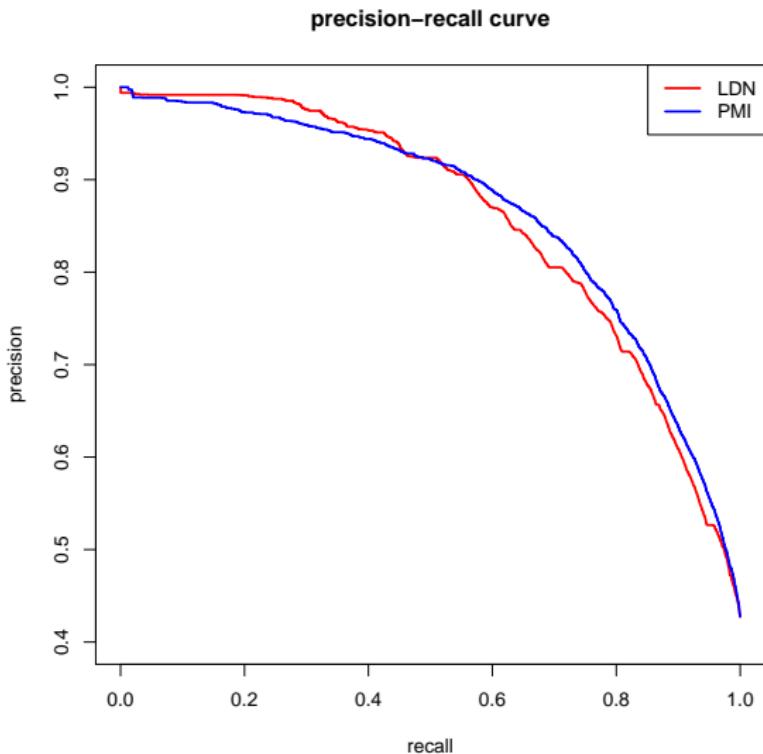
expert cognacy judgments used as gold standard



How well does PMI similarity predict cognacy?

Average Precision

- LDN: 0.847
- PMI: 0.864



Estimating distances from pairwise alignments

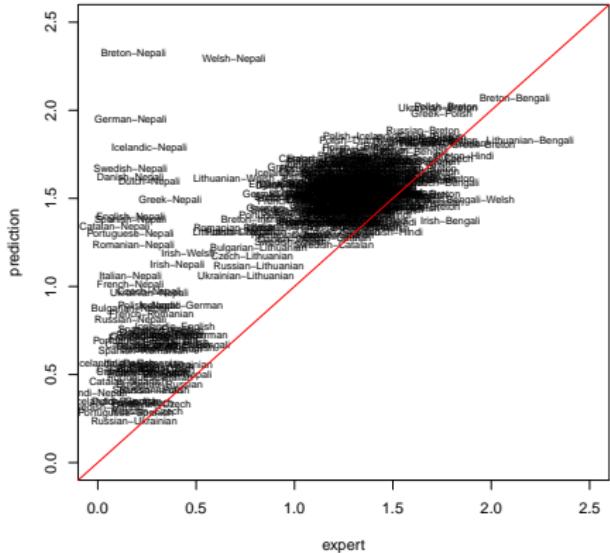
Probability of cognacy

- logistic regression to predict probability of cognacy from PMI similarity

| concept | Italian | English | predicted prob. | expert judgment | concept | Italian | English | predicted prob. | expert judgment |
|---------|-------------|---------|-----------------|-----------------|---------|-----------|---------|-----------------|-----------------|
| sharp | tallEnte | Sop | 0.004 | 0 | father | padre | fo83 | 0.480 | 1 |
| float | galleddZare | f13ut | 0.004 | 0 | when | kwando | wEn | 0.483 | 1 |
| Kill | ammattsare | kil | 0.007 | 0 | night | notte | nait | 0.508 | 1 |
| bark | skordza | bok | 0.009 | 0 | and | eed | End | 0.518 | 0 |
| husband | marito | hozb3nd | 0.010 | 0 | name | nome | neim | 0.519 | 1 |
| walk | kamminare | wok | 0.011 | 0 | worm | vErme | w3m | 0.521 | 1 |
| eat | mandZare | it | 0.011 | 0 | round | tondo | raund | 0.526 | 1 |
| bark | kortettSa | bok | 0.013 | 0 | many | molti | mEni | 0.569 | 0 |
| know | sapere | n3u | 0.015 | 0 | wind | vEnto | wind | 0.573 | 1 |
| come | venire | kom | 0.016 | 1 | two | due | tu | 0.600 | 1 |
| swim | nwtware | swim | 0.016 | 0 | mother | madre | mo83 | 0.624 | 1 |
| back | dosso | bEk | 0.018 | 0 | thou | tu | 8au | 0.629 | 1 |
| burn | ardere | b3n | 0.018 | 0 | child | fantSullo | tSaild | 0.638 | 0 |
| think | pensare | 8iNk | 0.019 | 0 | long | lungo | loN | 0.651 | 1 |
| dust | polvere | dost | 0.019 | 0 | fish | peSSe | fiS | 0.659 | 1 |
| wife | molle | waif | 0.020 | 0 | count | kontare | kaunt | 0.660 | 1 |
| swell | gonfyare | swEl | 0.021 | 0 | star | stella | sto | 0.664 | 1 |
| sing | kantare | siN | 0.022 | 0 | belly | vEntre | bEli | 0.679 | 0 |
| knee | rotElla | ni | 0.022 | 0 | sun | sole | son | 0.692 | 1 |
| dry | aSSutto | drai | 0.022 | 0 | fly | volare | flai | 0.742 | 0 |
| five | tSinkwe | faiv | 0.023 | 1 | three | tre | 8ri | 0.744 | 1 |
| skin | pElle | skin | 0.024 | 0 | flow | fluire | f13u | 0.759 | 0 |
| hand | mano | hEnd | 0.025 | 0 | heavy | grEve | hEvi | 0.769 | 0 |
| blood | sangwe | blod | 0.025 | 0 | person | persona | p3s3n | 0.799 | 1 |
| flow | skorrere | f13u | 0.026 | 0 | animal | animale | Enim3l | 0.947 | 1 |
| wipe | aSSugare | waip | 0.026 | 0 | vomit | vomitare | vomit | 0.960 | 1 |
| turn | dZirare | t3n | 0.026 | 0 | fruit | frutto | frut | 0.966 | 1 |

Estimating distances

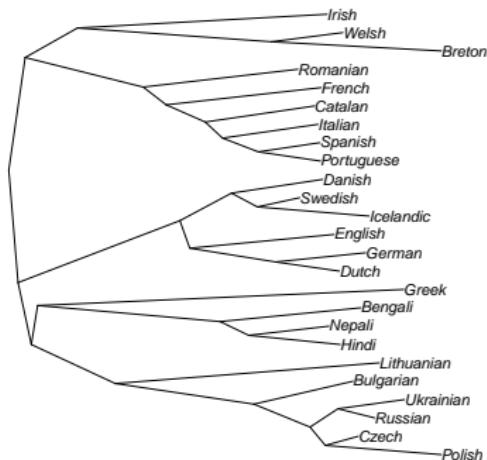
- average or maximal predicted probability of cognacy per concept = expected relative frequency of cognate pairs
- expected relative frequency of cognate pairs = e^{-t}
- ⇒ distance estimation from raw data
- ⇒ applicable across language families



Estimating distances

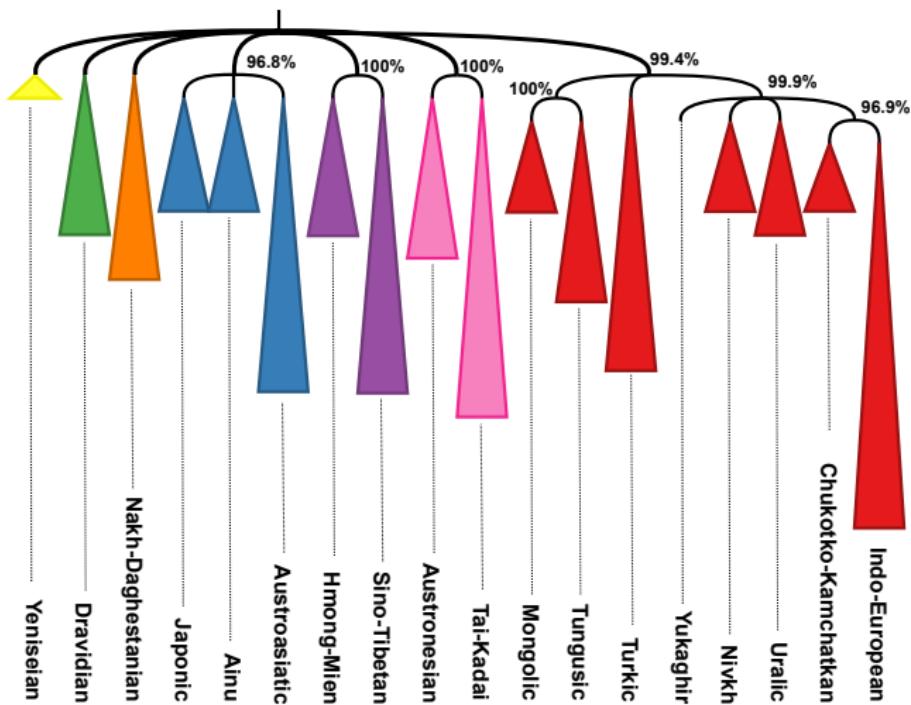
- average or maximal predicted probability of cognacy per concept = expected relative frequency of cognate pairs
- expected relative frequency of cognate pairs = e^{-t}
- ⇒ distance estimation from raw data
- ⇒ applicable across language families

Neighbor Joining tree



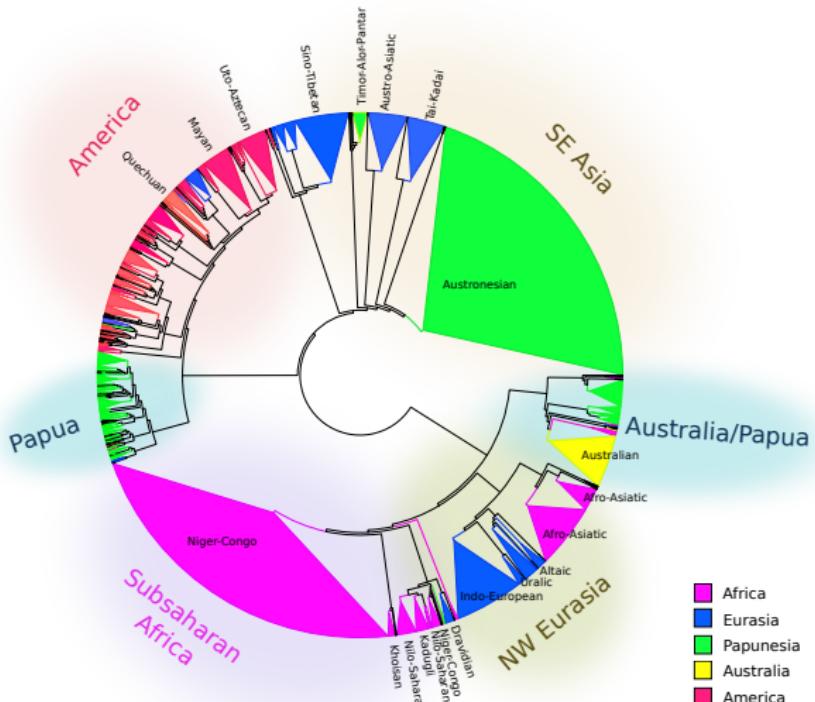
Languages of Eurasia / ASJP data

cf. Jäger (2015); full tree can be inspected [here](#)



Languages of the World/ ASJP data

cf. Jäger and Wichmann (2016); full tree can be inspected [here](#).



Multiple sequence alignment

Multiple sequence alignment

- Needleman-Wunsch only does pairwise alignment
- desirable: aligning all sequences of a taxon into one matrix
 - necessary for character-based phylogenetic inference
 - improves the quality of the alignment

Multiple sequence alignment

- example: 'one'
 - PIE: oinos
 - Bosian: yedan
 - Kashubian: yEdEn
 - optimal pairwise alignments:

| | | | | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| o | i | n | o | s | o | i | n | o | s | y | e | d | a | n |
| y | e | d | a | n | y | E | d | E | n | y | E | d | E | n |

- optimal multiple alignment (maximizing sum of pairwise similarities per column):

| | | | | | | |
|---|---|---|---|---|---|---|
| y | E | d | E | n | - | - |
| - | o | - | i | n | o | s |
| y | e | d | a | n | - | - |

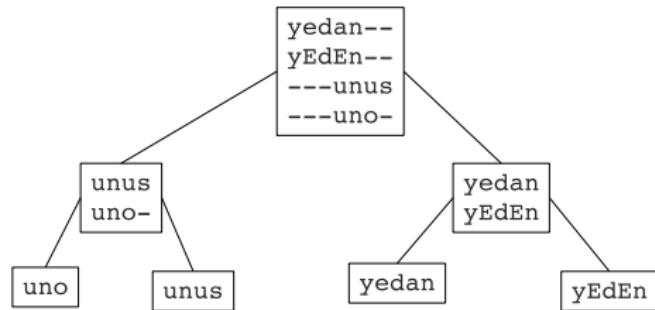
- alignment of all 'n's is etymologically correct

Multiple sequence alignment

- in principle, the Needleman-Wunsch algorithm can be generalized to aligning k sequences
- however, aligning k sequences of length n has complexity $\mathcal{O}(n^{k^2}) \Rightarrow$ computationally intractable
- two strategies
 - heuristic search
 - progressive alignment

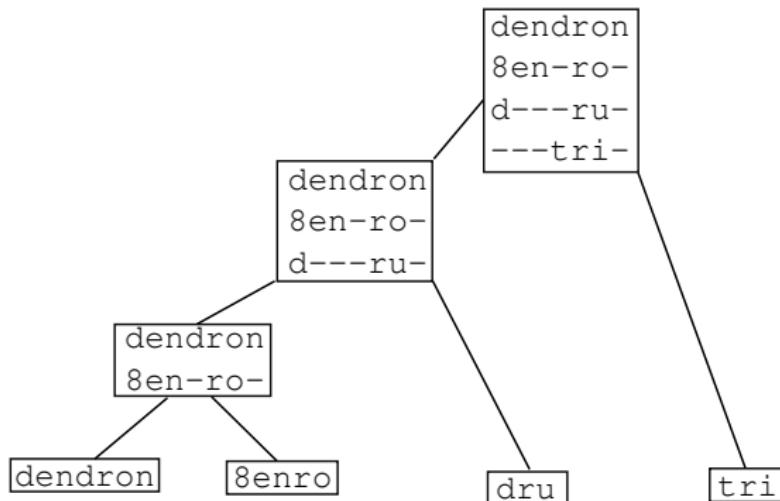
Progressive sequence alignment

- start with a **guide tree** (using some heuristics like pairwise alignment + Neighbor Joining)
- working bottom-up, at each internal node, do pairwise alignment of the block alignments at the daughter node
- complexity is $\mathcal{O}(n^2k^3) \Rightarrow$ computationally feasible



T-Coffee

- progressive alignment only uses (phylogenetically) local information
- erroneous decisions cannot be corrected later



T-Coffee

Tree-based Consistency Objective Function for alignment Evaluation (Notredame et al., 2000)

(slightly adapted for linguistic application)

- ① pairwise alignment for all word pairs, using PMI scores

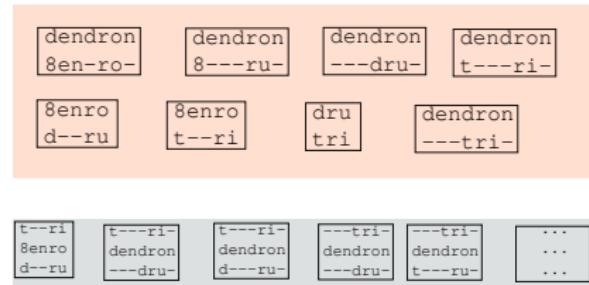
| | | | |
|---------|---------|---------|---------|
| dendron | dendron | dendron | dendron |
| 8en-ro- | 8---ru- | ---dru- | t---ri- |
| 8enro | 8enro | dru | dendron |
| d--ru | t--ri | tri | ---tri- |

T-Coffee

Tree-based Consistency Objective Function for alignment Evaluation (Notredame et al., 2000)

(slightly adapted for linguistic application)

- ① pairwise alignment for all word pairs, using PMI scores
- ② ternary alignments via relation composition

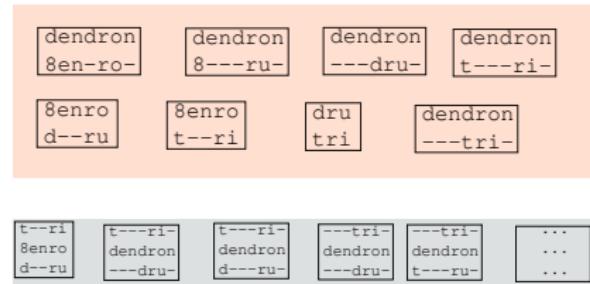


T-Coffee

Tree-based Consistency Objective Function for alignment Evaluation (Notredame et al., 2000)

(slightly adapted for linguistic application)

- ① pairwise alignment for all word pairs, using PMI scores
- ② ternary alignments via relation composition
- ③ indirect alignment scores between sound **occurrences**

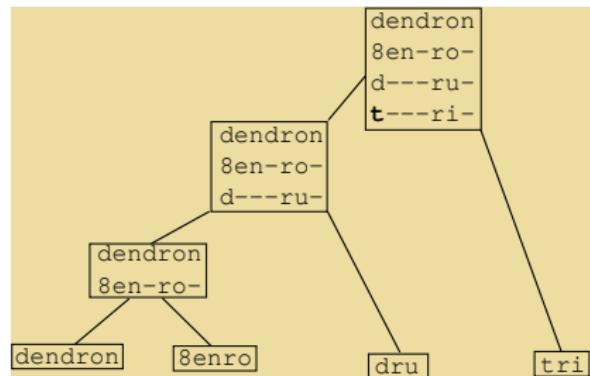


T-Coffee

Tree-based Consistency Objective Function for alignment Evaluation (Notredame et al., 2000)

(slightly adapted for linguistic application)

- ① pairwise alignment for all word pairs, using PMI scores
- ② ternary alignments via relation composition
- ③ indirect alignment scores between sound **occurrences**
- ④ progressive alignment using those scores



Examples

| cognate class | language | word |
|---------------|------------|----------|
| one:A | German | -a-i--n- |
| one:A | Dutch | ---e--n- |
| one:A | English | -w-o--n- |
| one:A | Danish | ---e--n- |
| one:A | Swedish | ---E--n- |
| one:A | Icelandic | ---eidn- |
| one:A | Irish | ---e--n- |
| one:A | Breton | ---i--n- |
| one:A | French | ---E---- |
| one:A | Catalan | ---u--n- |
| one:A | Spanish | ---u--no |
| one:A | Portuguese | ---u---- |
| one:A | Italian | ---u--no |
| one:A | Romanian | ---u--nu |
| one:A | Bengali | ---E--k- |
| one:A | Nepali | ---e--k- |
| one:A | Czech | yEdE--n- |
| one:A | Polish | yEdE--n- |
| one:A | Ukrainian | -odi--n- |
| one:A | Russian | -adi--n- |
| one:A | Bulgarian | -3di--n- |

| cognate class | language | word |
|---------------|------------|------------|
| heart:J | German | h-Er-t--s- |
| heart:J | Dutch | h-or-t---- |
| heart:J | English | h-o--t---- |
| heart:J | Danish | y-Ea-d--3- |
| heart:J | Swedish | y-E--t--a- |
| heart:J | Icelandic | S-ar-t--a- |
| heart:J | French | k-Er----- |
| heart:J | Catalan | k-or----- |
| heart:J | Spanish | k-ora8--on |
| heart:J | Portuguese | k-uras--aw |
| heart:J | Italian | kwor----e- |
| heart:J | Hindi | h--r-d--ai |
| heart:J | Lithuanian | S-ir-dis-- |
| heart:J | Czech | s--r-t-sE- |
| heart:J | Polish | s-Er-t-sE- |
| heart:J | Ukrainian | s-Er-t-sE- |
| heart:J | Russian | s-Erdt-sE- |
| heart:J | Bulgarian | s-3r-t-sE- |
| heart:J | Greek | k-ar-8-Sa- |

Examples

| cognate class | language | word |
|---------------|------------|--------|
| two:A | German | tsvai- |
| two:A | Dutch | t-we-- |
| two:A | English | t--u-- |
| two:A | Danish | d--o-- |
| two:A | Swedish | t-vo-- |
| two:A | Icelandic | t-veir |
| two:A | French | d--e-- |
| two:A | Catalan | d--o-s |
| two:A | Spanish | d--o-s |
| two:A | Portuguese | d--oiS |
| two:A | Italian | d--ue- |
| two:A | Romanian | d--o-y |
| two:A | Nepali | d--ui- |
| two:A | Czech | d-va-- |
| two:A | Polish | d-va-- |
| two:A | Ukrainian | d-wa-- |
| two:A | Russian | d-va-- |
| two:A | Bulgarian | d-va-- |
| two:A | Greek | 8-io-- |

| cognate class | language | word |
|---------------|------------|----------|
| mother:A | German | mu-t--a- |
| mother:A | Dutch | mu-d--3r |
| mother:A | English | mo-8--3- |
| mother:A | Danish | mo----a- |
| mother:A | Swedish | mu-d--3r |
| mother:A | Icelandic | mou8--ir |
| mother:A | French | mE---r-- |
| mother:A | Catalan | ma---r3- |
| mother:A | Spanish | ma-8-re- |
| mother:A | Portuguese | ma----i- |
| mother:A | Italian | ma-d-re- |
| mother:A | Czech | ma-t-ka- |
| mother:A | Polish | ma-t-ka- |
| mother:A | Ukrainian | ma-t--i- |
| mother:A | Russian | ma-t---- |
| mother:A | Bulgarian | ma-y-k3- |
| mother:A | Greek | mi-tera- |

Examples

| cognate class | language | word |
|-----------------|------------|------------|
| <i>tongue:W</i> | German | ---tsuN--3 |
| <i>tongue:W</i> | Dutch | ---t-oN--- |
| <i>tongue:W</i> | English | ---t-oN--- |
| <i>tongue:W</i> | Danish | ---d-oN--3 |
| <i>tongue:W</i> | Swedish | ---t-3N--a |
| <i>tongue:W</i> | Icelandic | ---t-uNg-a |
| <i>tongue:W</i> | French | ---l-o-g-- |
| <i>tongue:W</i> | Catalan | ---l-ENgw3 |
| <i>tongue:W</i> | Spanish | ---l-eNgwa |
| <i>tongue:W</i> | Portuguese | ---l-i-gua |
| <i>tongue:W</i> | Italian | ---l-ingwa |
| <i>tongue:W</i> | Romanian | ---l-im-b3 |
| <i>tongue:W</i> | Hindi | ---dZi--b- |
| <i>tongue:W</i> | Czech | ya-z-ik--- |
| <i>tongue:W</i> | Polish | yEzw-3k--- |
| <i>tongue:W</i> | Ukrainian | ya-z-ik--- |
| <i>tongue:W</i> | Russian | yi-z-3k--- |
| <i>tongue:W</i> | Bulgarian | -3-z-ik--- |

| cognate class | language | word |
|----------------|------------|--------|
| <i>tooth:B</i> | Greek | 8-ondi |
| <i>tooth:B</i> | German | tsan-- |
| <i>tooth:B</i> | Dutch | t-ont- |
| <i>tooth:B</i> | English | t-u-8- |
| <i>tooth:B</i> | Danish | d-an-- |
| <i>tooth:B</i> | Swedish | t-and- |
| <i>tooth:B</i> | Icelandic | t-En-- |
| <i>tooth:B</i> | French | d-o--- |
| <i>tooth:B</i> | Catalan | d-en-- |
| <i>tooth:B</i> | Spanish | dyente |
| <i>tooth:B</i> | Portuguese | d-e-t3 |
| <i>tooth:B</i> | Italian | d-Ente |
| <i>tooth:B</i> | Romanian | d-inte |
| <i>tooth:B</i> | Bengali | d-o-t- |
| <i>tooth:B</i> | Hindi | d-a-t- |

Examples

| cognate class | language | word |
|---------------|------------|----------|
| dog:A | Lithuanian | S-u---o- |
| dog:A | Ukrainian | s-obaka- |
| dog:A | Russian | s-abaka- |
| dog:A | Danish | h-u-n--- |
| dog:A | Swedish | h-3-nd-- |
| dog:A | Icelandic | h-i-ndir |
| dog:A | German | h-u-nt-- |
| dog:A | Dutch | h-o-nt-- |
| dog:A | Welsh | k-----i- |
| dog:A | Breton | k-----i- |
| dog:A | Irish | k-----u- |
| dog:A | French | S-i---E- |
| dog:A | Italian | k-a-n-e- |
| dog:A | Portuguese | k-a---u- |
| dog:A | Romanian | k-3yn-e- |
| dog:A | Greek | Tio-n--- |

| cognate class | language | word |
|---------------|-----------|------------|
| tree:C | Danish | d---G-E-- |
| tree:C | Swedish | t---r-Ed- |
| tree:C | Icelandic | t---ryE-- |
| tree:C | English | t---r-i-- |
| tree:C | Ukrainian | dE--r-Ewo |
| tree:C | Russian | dE--r-Evo |
| tree:C | Polish | d---Z-Evo |
| tree:C | Bulgarian | d3---r--vo |
| tree:C | Greek | 8endr---o |

Wrapping up

Important topics not covered

- Bayesian tree estimation ⇒ no good introductory texts so far (that I would be aware of); best starting point might be Chen et al. (2014), esp. chapters 1 and 7
- estimation of time depths in years (rather than in “expected number of mutations”) ⇒ Chang et al. (2015)
- automatic cognate detection ⇒ first part of the Jäger/List-manuscript on the course homepage

Hot research topics

- automatic discovery of regular sound correspondences and sound laws
- automatic reconstruction of proto-forms
- factoring vertical descent from language contact
- integrated probabilistic inference of sequence alignment and phylogenies

- Chang, W., C. Cathcart, D. Hall, and A. Garrett (2015). Ancestry-constrained phylogenetic analysis supports the Indo-European steppe hypothesis. *Language*, **91**(1):194–244.
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- Dolgopolsky, A. B. (1986). A probabilistic hypothesis concerning the oldest relationships among the language families of northern eurasia. In V. V. Shevoroshkin, ed., *Typology, Relationship and Time: A collection of papers on language change and relationship by Soviet linguists*, pp. 27–50. Karoma Publisher, Ann Arbor.
- Jäger, G. (2015). Support for linguistic macrofamilies from weighted sequence alignment. *Proceedings of the National Academy of Sciences*, **112**(41):12752–12757. Doi: [10.1073/pnas.1500331112](https://doi.org/10.1073/pnas.1500331112).
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